

# Experiments with spin qubits in silicon and diamond

Gavin W Morley  
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## Experiments with spin qubits in silicon and diamond: overview

- Lecture 1
  - Magnetic resonance
  - Silicon
- Lecture 2
  - Silicon (cont.)
- Lecture 3
  - Diamond

← **Lab tours  
Friday  
morning**



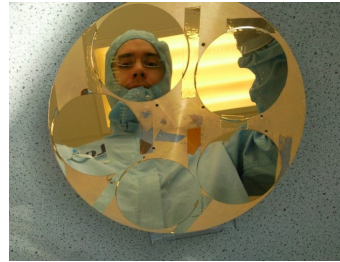
# Experiments with spin qubits in silicon and diamond: overview

- Lecture 1

- Magnetic resonance

1. Prepare (spin Hamiltonian)
2. Control (electromagnetic pulses)
3. Measure (spin state readout)

- Silicon



- Magnetic resonance

1. Prepare (spin Hamiltonian)
2. Control (electromagnetic pulses)
3. Measure (spin state readout)



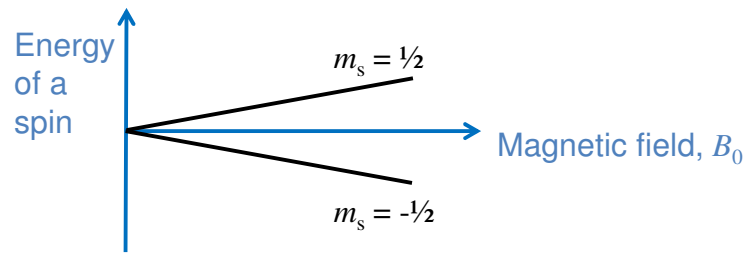
Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015

## Magnetic resonance: prepare

- put a spin  $\frac{1}{2}$  into a magnetic field

Hamiltonian  $\mathcal{H} = \omega_S \hat{S}_Z$

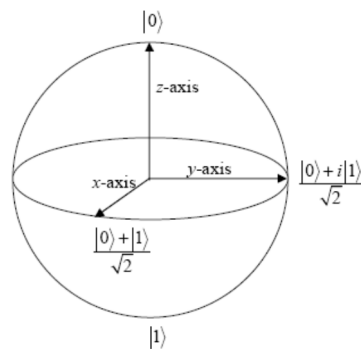
with energy,  $\hbar \omega_S = g \mu_B B_0$   
 for  $g$ -factor,  $g \sim 2$ ,  
 Bohr magneton  $\mu_B = e \hbar / 2m_e$ ,  
 electron spin  $S = \frac{1}{2}$



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## Magnetic resonance: prepare

- put a spin  $\frac{1}{2}$  into a magnetic field

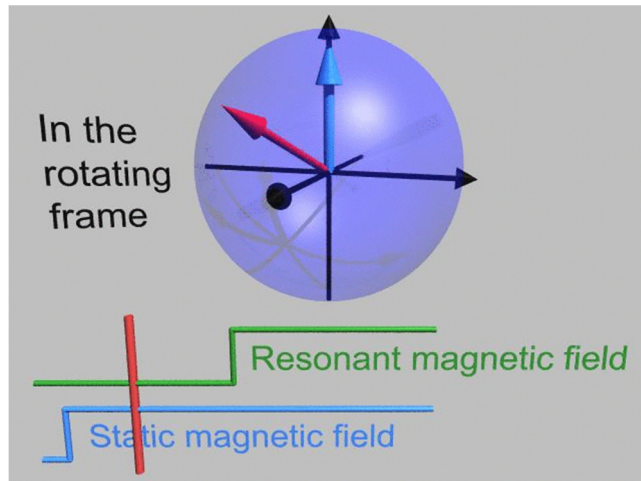


Larmor  
precession at  
angular  
frequency  $\omega_S$

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## Magnetic resonance: prepare

- put a spin  $\frac{1}{2}$  into a magnetic field



Larmor precession at angular frequency  $\omega_S$

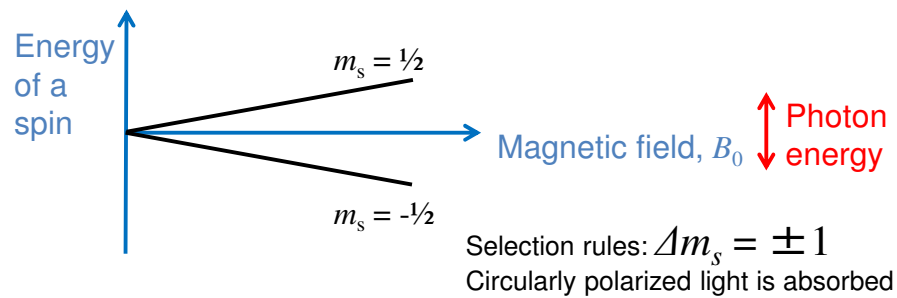
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## Magnetic resonance: control

- send in electromagnetic radiation

Energy gap is  $\Delta E = g \mu_B B_0$   
magnetic resonance occurs when photon energy

$$\hbar \omega_S = \Delta E$$



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## Magnetic resonance: measure

- spin readout

- Large ensembles
  - Precessing magnetic moments induce current in a coil (standard for NMR of  $>10^{15}$  nuclei)
  - Detect microwave power absorbed or emitted (standard for ESR of  $>10^9$  electron spins)
- Single spins
  - Electrically (eg in silicon)
  - Optically (eg in diamond)

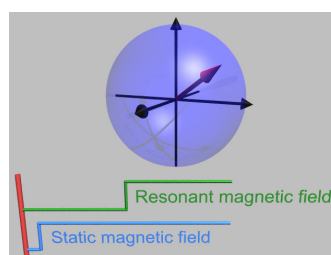
Footnote: the terms electron spin resonance (ESR) and electron paramagnetic resonance (EPR) are used interchangeably

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## Magnetic resonance

Mini-summary:

1. Prepare (spin Hamiltonian)
2. Control (electromagnetic pulses)
3. Measure (spin state readout)



References:

MR for QIP theorists: MH Mohammady, PhD thesis, Chapter 3, UCL (2012)

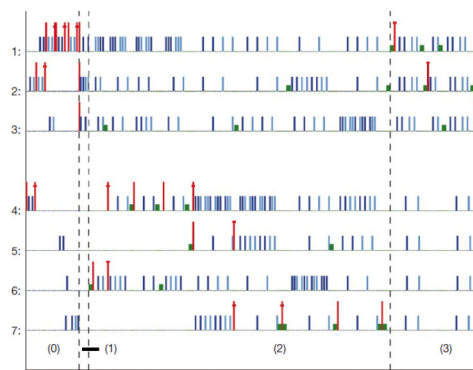
ESR: A Schweiger & G Jeschke, *Principles of Pulse Electron Paramagnetic Resonance* (Oxford University Press, Oxford, 2001)

NMR: MH Levitt, *Spin Dynamics* (Wiley, 2001)

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## Magnetic resonance for QIP

### Pioneering work: liquid-state NMR QIP



LMK Vandersypen *et al*,  
*Experimental realization of  
Shor's quantum factoring  
algorithm using nuclear  
magnetic resonance*, *Nature*  
**414**, 883 (2001)

WS Warren, *The usefulness  
of NMR quantum  
computing*, *Science* **277**,  
1688 (1997).

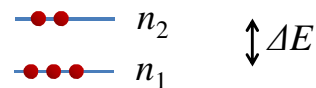
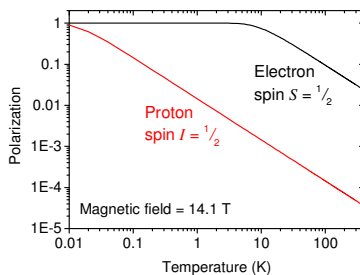
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## Magnetic resonance for QIP

### Pioneering work: liquid-state NMR QIP

Mini-summary:

1. Prepare (pseudo-pure state)
2. Control (NMR pulses)
3. Measure (spin state of large ensemble)



At thermal equilibrium:  
 $n_2/n_1 = \exp(-\Delta E / k_B T)$

Define polarization as:  
 $P = (n_1 - n_2) / (n_1 + n_2)$

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## Magnetic resonance for QIP

### Pioneering work: liquid-state NMR QIP

...pseudo-pure states

$$\rho_{\text{thermalized}} = N \begin{pmatrix} p_1 & 0 & 0 & \cdots & 0 \\ 0 & p_2 & 0 & \cdots & 0 \\ 0 & 0 & p_3 & \cdots & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & 0 & 0 & p_m \end{pmatrix}$$

$$p_i = \frac{e^{-\frac{E_i}{k_B T}}}{\sum_{j=1}^m e^{-\frac{E_j}{k_B T}}}$$

$$p_1 = \frac{e^{-\frac{E_1}{k_B T}}}{\sum_{j=1}^m e^{-\frac{E_j}{k_B T}}} \approx \frac{1 - \frac{E_1}{k_B T}}{m}$$

---


$$\rho_{\text{pseudo}} = N \begin{pmatrix} p_1 & 0 & 0 & \cdots & 0 \\ 0 & \bar{p} & 0 & \cdots & 0 \\ 0 & 0 & \bar{p} & \cdots & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & 0 & 0 & \bar{p} \end{pmatrix} = N\bar{p} \begin{pmatrix} 1 & 0 & 0 & \cdots & 0 \\ 0 & 1 & 0 & \cdots & 0 \\ 0 & 0 & 1 & \cdots & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix} + N(p_1 - \bar{p}) \begin{pmatrix} 1 & 0 & 0 & \cdots & 0 \\ 0 & 0 & 0 & \cdots & 0 \\ 0 & 0 & 0 & \cdots & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

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## Magnetic resonance for QIP

### Pioneering work: liquid-state NMR QIP

...pseudo-pure states

$$N(p_1 - \bar{p}) \approx \frac{-\frac{NE_1}{k_B T}}{2q - 1}$$

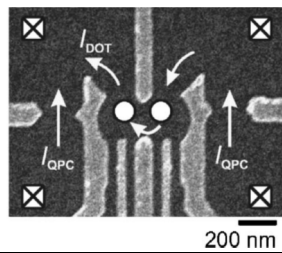
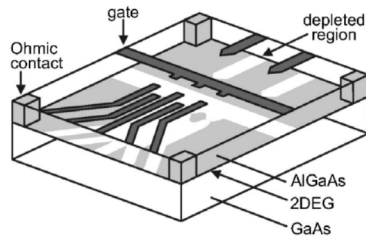
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$$\rho_{\text{pseudo}} = N \begin{pmatrix} p_1 & 0 & 0 & \cdots & 0 \\ 0 & \bar{p} & 0 & \cdots & 0 \\ 0 & 0 & \bar{p} & \cdots & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & 0 & 0 & \bar{p} \end{pmatrix} = N\bar{p} \begin{pmatrix} 1 & 0 & 0 & \cdots & 0 \\ 0 & 1 & 0 & \cdots & 0 \\ 0 & 0 & 1 & \cdots & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix} + N(p_1 - \bar{p}) \begin{pmatrix} 1 & 0 & 0 & \cdots & 0 \\ 0 & 0 & 0 & \cdots & 0 \\ 0 & 0 & 0 & \cdots & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

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## Magnetic resonance for QIP

Pioneering work: GaAs quantum dots



**GaAs is a semiconductor ie  
"a place where electrons can  
be individuals"**

200  $\mu$ s spin coherence time:  
H Bluhm *et al*, Nature Physics  
**7**, 109 (2011)

R Hanson *et al*, Reviews of  
Modern Physics **79**, 1217  
(2007)

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## Magnetic resonance for QIP

Use electron spins in semiconductors which have  
a low background of nuclear spins:

Silicon and Diamond

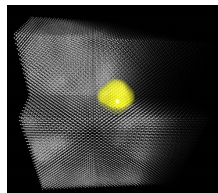


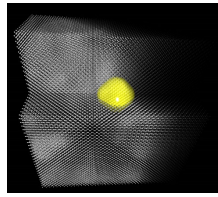
Image by Manuel Vögtli



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## Donors in silicon



Group	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18														
Period 1	1 H																		2 He													
Period 2	3 Li	4 Be											5 B	6 C	7 N	8 O	9 F	10 Ne														
Period 3	11 Na	12 Mg											13 Al	14 Si	15 P	16 S	17 Cl	18 Ar														
Period 4	19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr														
Period 5	37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe														
Period 6	55 Cs	56 Ba	57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn
Period 7	87 Fr	88 Ra	89 Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Uub	113 Uut	114 Uuq	115 Uup	116 Uuq	117 Uus	118 Uuo
Lanthanides	57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu																	
Actinides	89 Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr																	

Metals

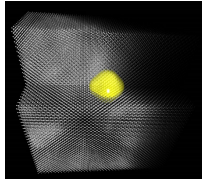
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## Donors in silicon



5 B	6 C	7 N	8 O
13 Al	14 Si	15 P	16 S
31 Ga	32 Ge	33 As	34 Se
49 In	50 Sn	51 Sb	52 Te
81 Tl	82 Pb	83 Bi	84 Po
113 Nh	114 Fl	115 Mc	116 Lv

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## Donors in silicon

- Hydrogenic model

Solve Schrödinger's equation for an electron in a box:  $-\frac{\hbar^2}{2m_e} \left( \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2} \right) \Psi + V\Psi = E\Psi$

Relative permittivity,  $\epsilon_r$   
Effective mass,  $m^*$

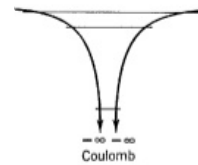
W Kohn, Shallow Impurity States in Silicon and Germanium, Solid State Physics 5, 257 (Academic, New York 1957)

Coulomb potential:  $V = -\frac{e^2}{4\pi\epsilon_0 r}$

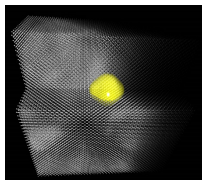
$^1\text{H}$  energy levels:  $E = -\frac{13.6 \text{ eV}}{n^2}$

Donor energy levels:

$$E = \frac{-m^*}{m_e} \frac{1}{\epsilon_r^2} \frac{13.6 \text{ eV}}{n^2}$$

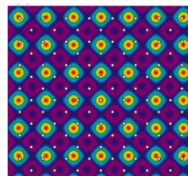


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## Donors in silicon

- Hydrogenic model



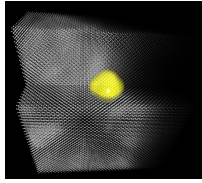
B Koiller, RB Capaz, X Hu and S Das Sarma, PRB **70**, 115207 (2004)

	Relative permittivity, $\epsilon_r$	$m^*/m_e$	Binding energy for phosphorous dopant (meV)
Silicon	11.7	0.98 (long.) 0.19 (trans.)	46
Diamond	5.5 - 10	1.4 (long.) 0.36 (trans.)	500

Donor energy levels:

$$E = \frac{-m^*}{m_e} \frac{1}{\epsilon_r^2} \frac{13.6 \text{ eV}}{n^2}$$

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## Donors in silicon

$$\mathcal{H} = \omega_S \hat{S}_z - \omega_I \hat{I}_z + A \hat{S} \cdot \hat{I}$$

with electron spin  $S = 1/2$  and nuclear spin:

$I = 1/2$  for phosphorous (Si:P)

$I = 3/2$  for arsenic (Si:As)

$I = 5/2$  or  $7/2$  for antimony (Si:Sb)

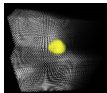
$I = 9/2$  for bismuth (Si:Bi)



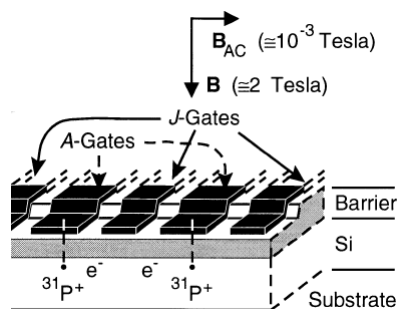
Pioneering early work:

- G Feher and EA Gere, Physical Review **114**, 1245 (1959)
- G Feher, Physical Review **114**, 1219 (1959)
- JP Gordon and KD Bowers, Physical Review Letters **1**, 368 (1958)

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## Donor qubits in silicon



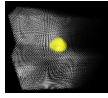
Kane proposal:

BE Kane, *A silicon-based nuclear spin quantum computer*, Nature **393**, 133 (1998)

Recent silicon QIP reviews:

- DD Awschalom *et al*, *Quantum Spintronics: Engineering and Manipulating Atom-Like Spins in Semiconductors*, Science **339**, 1174 (2013)
- FA Zwanenburg *et al*, *Silicon quantum electronics*, Rev Mod Phys **85**, 961 (2013)
- GW Morley, *Towards Spintronic Quantum Technologies with Dopants in Silicon*, book chapter in SPR Electron Paramagnetic Resonance Volume 24, arXiv1407.6250 (2014)

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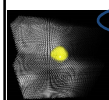


## Donor qubits in silicon

### Mini-overview

- Atomically-precise device fabrication
- Qubit initialisation
- Readout
- Control
- Coherence times

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Fabrication Initialisation Readout Control Coherence

## Atomically-precise fabrication

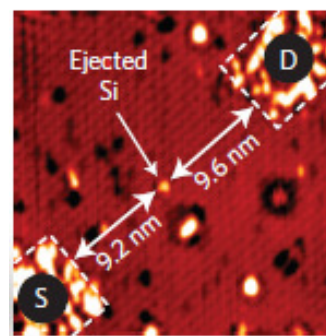
### Using scanning tunnelling microscopy (STM)

JL O'Brien *et al.*, PRB **64**, 161401 (2001)

SR Schofield *et al.*, PRL **91**, 136104 (2003)

M Fuechsle *et al.*, Nat Nano **7**, 242 (2012)

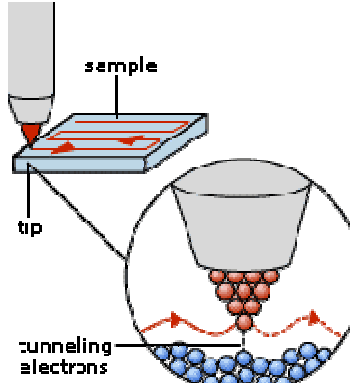
B Weber *et al.*, Science **335**, 64 (2012)



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Fabrication Initialisation Readout Control Coherence

# Scanning tunnelling microscopy (STM)




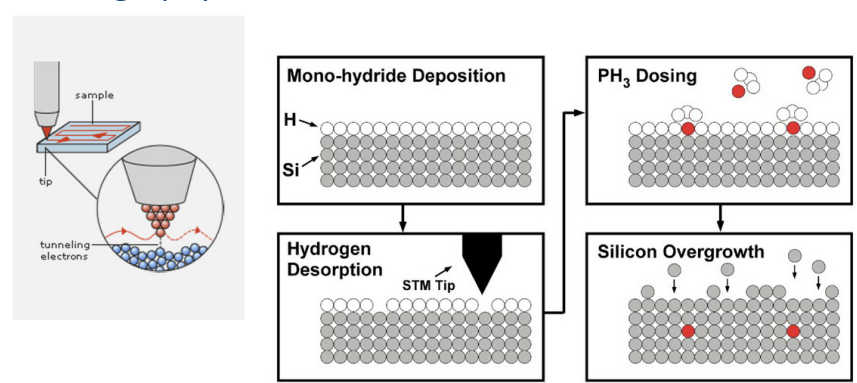
www.nobelprize.org/  
educational/physics/  
microscopes/scanning

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# Atomically-precise fabrication

Using STM and hydrogen lithography





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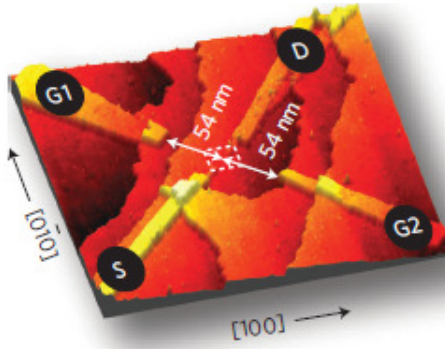
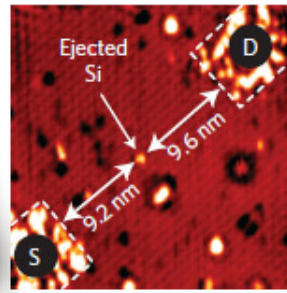
Fabrication
 Initialisation   Readout   Control   Coherence

## Atomically-precise fabrication

Using STM and hydrogen lithography



A Single Atom Transistor  
 M Fuechsle *et al.*, Nat Nano 7, 242 (2012)


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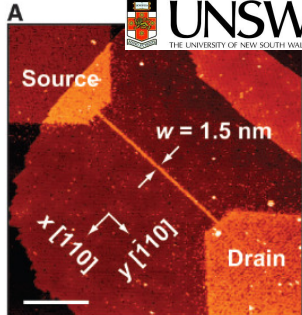
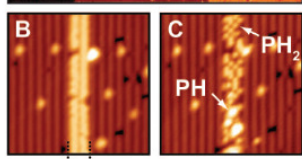
Fabrication
 Initialisation   Readout   Control   Coherence

## Atomically-precise fabrication

Using STM and hydrogen lithography

Ohm's law Survives to the Atomic Scale  
 B Weber *et al.*, Science 335, 64 (2012)



Two dimer rows

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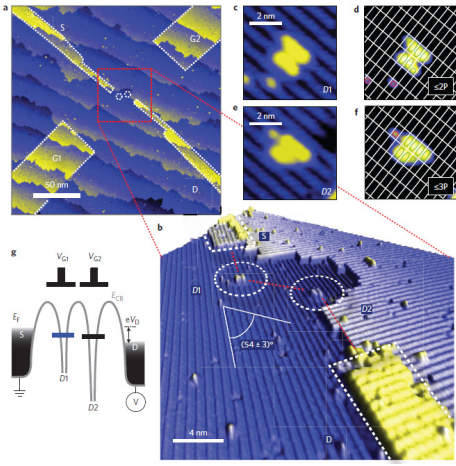
Fabrication **Initialisation** Readout Control Coherence

# Atomically-precise fabrication

Using STM and hydrogen lithography

Spin blockade and exchange in Coulomb-confined silicon double quantum dots  
 B Weber *et al.*, Nature Nano **9**, 430 (2014)

Remaining slides do not use STM or hydrogen lithography

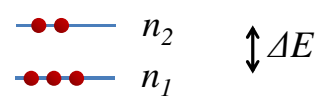
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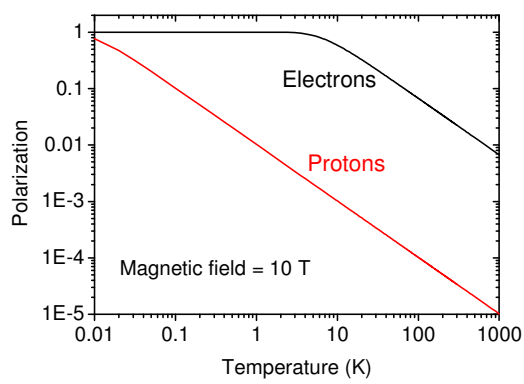
Fabrication **Initialisation** Readout Control Coherence

# Initialisation by spin polarization

Thermal (Boltzmann) equilibrium:  
 $n_2 / n_1 = \exp(-\Delta E / k_B T)$

Define polarization as:  
 $P = (n_1 - n_2) / (n_1 + n_2)$





DR McCamey, J van Tol, GW Morley and C Boehme, *Fast Nuclear Hyperpolarization of Phosphorus in Silicon*, Physical Review Letters, **102**, 027601 (2009)

Electron spin:  $P_{\text{Boltzmann}} = 99.9\%$ , Nuclear spin:  $P_{\text{measured}} = 68\%$

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Fabrication **Initialisation** Readout Control Coherence

## Qubit initialisation with lasers

A Yang *et al.*, *Simultaneous subsecond Hyperpolarization of the Nuclear and Electron Spins of Phosphorus in Silicon by Optical Pumping of Exciton Transitions*, *Physical Review Letters* **102**, 257401 (2009)

M Steger *et al.*, *Quantum Information Storage for over 180s Using Donor Spins in a <sup>28</sup>Si "Semiconductor Vacuum"*, *Science* **336**, 1280 (2012)

Electron spin:  $P_{\text{bound exciton}} = 97\%$   
 Nuclear spin:  $P_{\text{bound exciton}} = 90\%$

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Fabrication **Initialisation** Readout Control Coherence

## Initialisation by spin polarization

JT Muhonen *et al.*, *Storing quantum information for 30 seconds in a nanoelectronic device*, *Nature Nanotechnology*, **9**, 986 (2014)

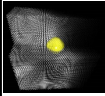
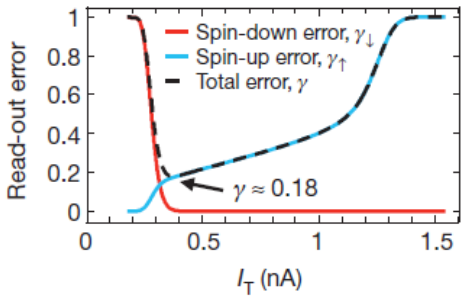
Electron spin:  $P_{\text{Boltzmann}} = 99.9999999\%$

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Fabrication **Initialisation** Readout Control Coherence

## Initialisation using a readout

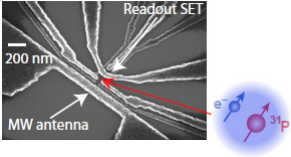



Read-out error

— Spin-down error,  $\gamma_{\downarrow}$   
— Spin-up error,  $\gamma_{\uparrow}$   
— Total error,  $\gamma$

$\gamma \approx 0.18$

$I_T$  (nA)



Readout SET  
200 nm  
MW antenna

UNSW  
THE UNIVERSITY OF NEW SOUTH WALES

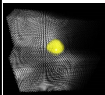
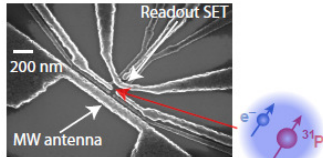
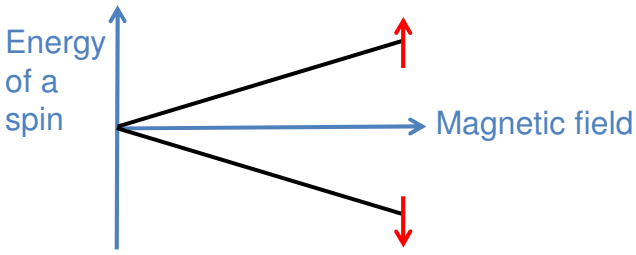
JJ Pla et al., *A single-atom electron spin qubit in silicon*, Nature **489**, 541 (2012)

Electron spin readout error  $\sim 18\%$   
Fast initialisation (spin-down) error  $\sim 1\%$

Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015

Fabrication Initialisation **Readout** Control Coherence

## Single-shot single-spin SET readout

Energy of a spin

Magnetic field

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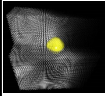
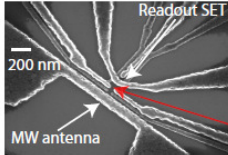
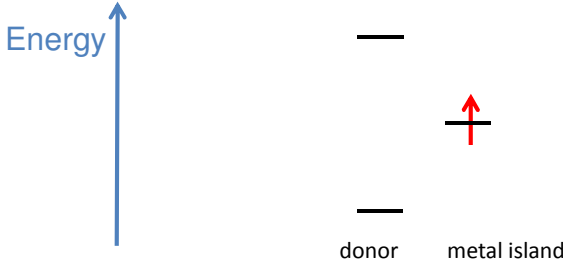
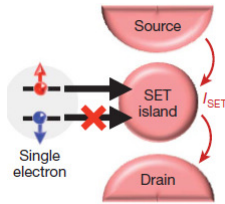
A Morello et al., *Single-shot readout of an electron spin in silicon*, Nature **467**, 687 (2010)

JJ Pla et al., *A single-atom electron spin qubit in silicon*, Nature **489**, 541 (2012)

Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015

Fabrication Initialisation **Readout** Control Coherence

# Single-shot single-spin SET readout

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A Morello *et al.*, *Single-shot readout of an electron spin in silicon*, Nature **467**, 687 (2010)

JJ Pla *et al.*, *A single-atom electron spin qubit in silicon*, Nature **489**, 541 (2012)

Energy ↑

donor metal island

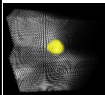
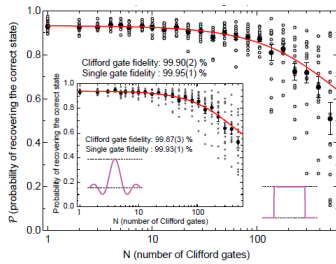
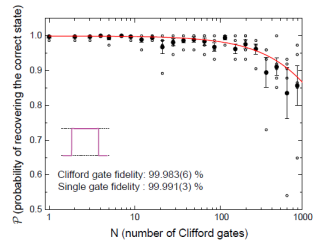
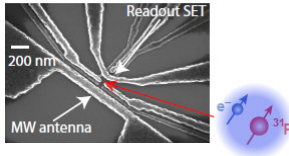
Source SET island Drain

Single electron  $I_{SET}$

Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015

Fabrication Initialisation Readout **Control** Coherence

# Qubit control

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JT Muhonen *et al.*, *Quantifying the quantum gate fidelity of single-atom spin qubits in silicon by randomized benchmarking*, arXiv:1410:2338

Average gate fidelities with  $^{28}\text{Si}$ :  
99.95% for electron  
99.99% for nucleus

Probability of recovering the correct state

Clifford gate fidelity: 99.90(2) %  
Single gate fidelity: 99.95(1) %

Clifford gate fidelity: 99.87(3) %  
Single gate fidelity: 99.93(1) %

Clifford gate fidelity: 99.983(6) %  
Single gate fidelity: 99.991(3) %

N (number of Clifford gates)

Readout SET

MW antenna

Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015

Fabrication Initialisation Readout **Control** Coherence

## Measuring coherence

spin echo decay

In rotating frame

Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015

Fabrication Initialisation Readout **Control** Coherence

## Coherence: donor qubit ensembles

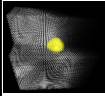
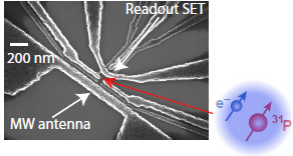

Nuclear  $T_2 = 3$  hours  
K Saeedi *et al.*, *Science* **342**, 830 (2013)

Electron  $T_2 > 1$  second  
AM Tyryshkin *et al.*, *Electron spin coherence exceeding seconds in high-purity silicon*, *Nature Materials* **11**, 143 (2012)

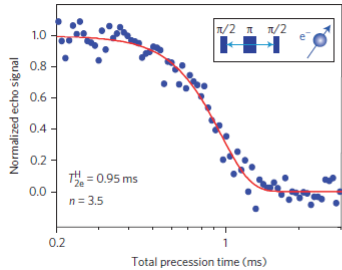
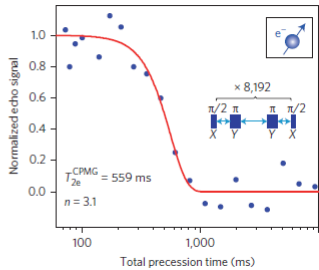
Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015

Fabrication Initialisation Readout Control **Coherence**

# Coherence of a single electron spin

Use <sup>28</sup>Si:  
 JT Muhonen *et al.*, *Storing quantum information for 30 seconds in a nanoelectronic device*, *Nature Nano* **9**, 986 (2014)

Normalized echo signal

Total precession time (ms)

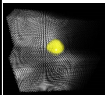
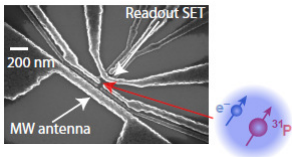

$T_{2e}^H = 0.95 \text{ ms}$   
 $n = 3.5$

$T_{2e}^{\text{CPMG}} = 559 \text{ ms}$   
 $n = 3.1$

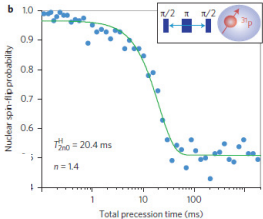
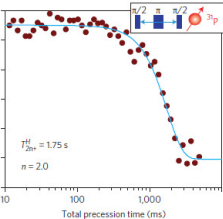
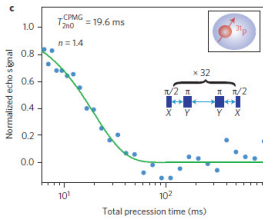
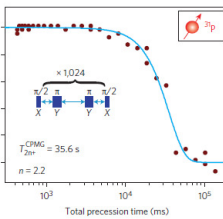
Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015

Fabrication Initialisation Readout Control **Coherence**

# Coherence of a single nuclear spin

Use <sup>28</sup>Si:  
 JT Muhonen *et al.*, *Storing quantum information for 30 seconds in a nanoelectronic device*, *Nature Nano* **9**, 986 (2014)

Nuclear spin flip probability

Total precession time (ms)

$T_{2n}^H = 20.4 \text{ ms}$   
 $n = 1.4$

$T_{2n}^H = 1.75 \text{ s}$   
 $n = 2.0$

Normalized echo signal

Total precession time (ms)

$T_{2n}^{\text{CPMG}} = 19.6 \text{ ms}$   
 $n = 1.4$

$T_{2n}^{\text{CPMG}} = 35.6 \text{ s}$   
 $n = 2.2$

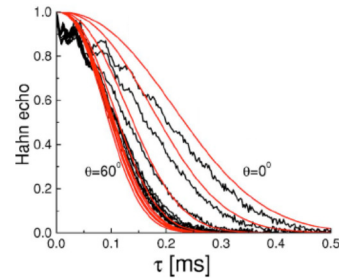
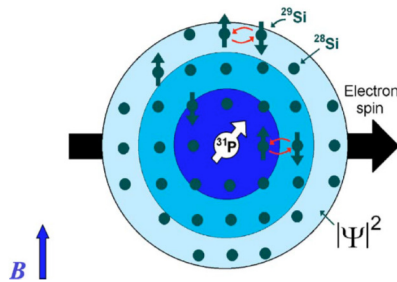
Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015

Fabrication Initialisation Readout Control **Coherence**

## Simulating coherence

Central spin problem: one electron spin in a bath of >1000 nuclear spins.  
Intractable to do a full quantum simulation with a classical computer.

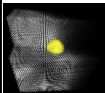
### Spectral diffusion of a Si:P spin



- WM Witzel & S Das Sarma, PRB **74**, 035322 (2006)
- W Yang & R-B Liu, PRB **78**, 085315 (2008)

Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015

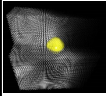
Fabrication Initialisation Readout Control Coherence



## Conclusions and perspective

Need to couple up two donors

Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015



## Bismuth donors in silicon

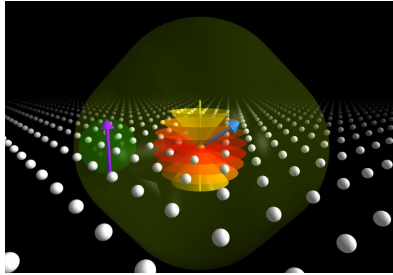
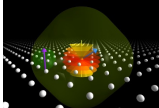


Image by Manuel Vögtli

T Sekiguchi *et al.*, PRL **104**, 137402 (2010)  
 GW Morley *et al.*, Nature Materials **9**, 725 (2010)  
 MH Mohammady, GW Morley & TS Monteiro, PRL **105**, 067602 (2010)  
 RE George *et al.*, PRL **105**, 067601 (2010)  
 GW Morley *et al.*, Nature Materials **12**, 103 (2013)  
 G Wolfowicz *et al.*, Nature Nano **8**, 561 (2013)

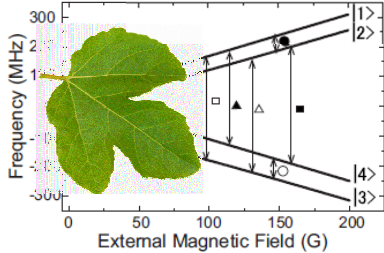
Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015



## Phosphorus qubits in silicon

$$\mathcal{H} = \omega_S \hat{S}_z - \omega_I \hat{I}_z + A \hat{S} \hat{I}$$

$$S = I = 1/2, \quad A/2\pi = 118 \text{ MHz}$$

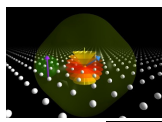
$$\beta = \sin \frac{\arctan\left(\frac{\hbar A/B}{g_e \mu_e - g_n \mu_n}\right)}{2}$$


Frequency (MHz)

External Magnetic Field (G)

$|1\rangle = |\uparrow\uparrow\rangle,$   
 $|2\rangle = \alpha|\uparrow\downarrow\rangle + \beta|\downarrow\uparrow\rangle,$   
 $|3\rangle = -\beta|\uparrow\downarrow\rangle + \alpha|\downarrow\uparrow\rangle,$   
 $|4\rangle = |\downarrow\downarrow\rangle$

Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015

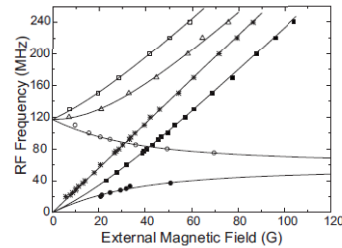
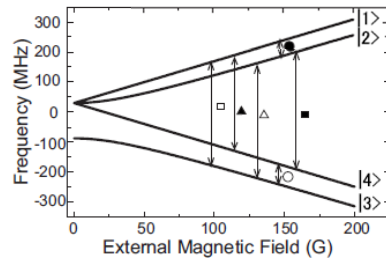


## Phosphorus qubits in silicon

$$\mathcal{H} = \omega_S \hat{S}_z - \omega_I \hat{I}_z + A \hat{S} \hat{I}$$

$$S = I = 1/2, \quad A/2\pi = 118 \text{ MHz}$$

H. Morishita, L. S. Vlasenko, H. Tanaka, K. Semba, K. Sawano, Y. Shiraki, M. Eto & K. M. Itoh, *Physical Review B* **80**, 205206 (2009).

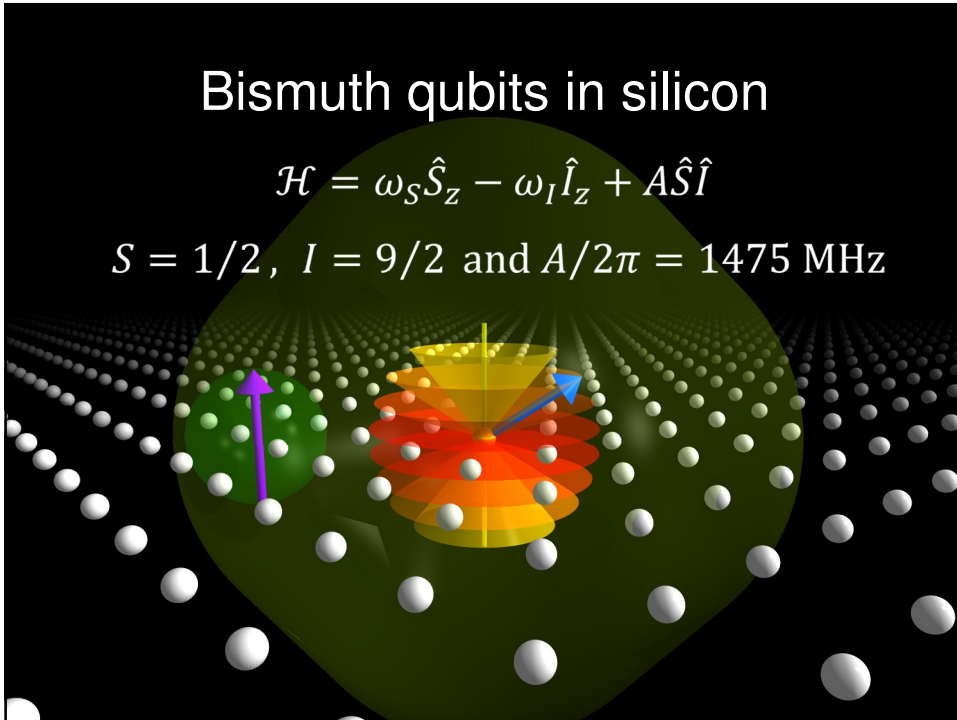


Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015

## Bismuth qubits in silicon

$$\mathcal{H} = \omega_S \hat{S}_z - \omega_I \hat{I}_z + A \hat{S} \hat{I}$$

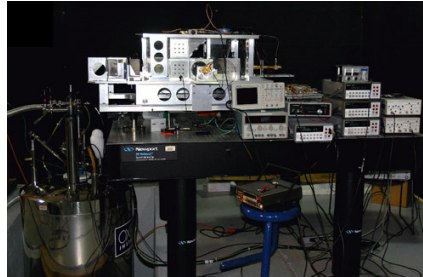
$$S = 1/2, \quad I = 9/2 \text{ and } A/2\pi = 1475 \text{ MHz}$$



## Pulsed electron spin resonance (ESR) at 110 – 336 GHz, 12.5 T

GWM, L-C Brunel & J van Tol, Rev Sci Instrum **79**, 064703 (2008)

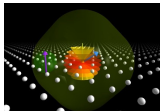
CW & transient EPR: J van Tol, L-C Brunel & R J Wylde, Rev Sci Instrum **76**, 074101 (2005)



99.9% electron spin polarization

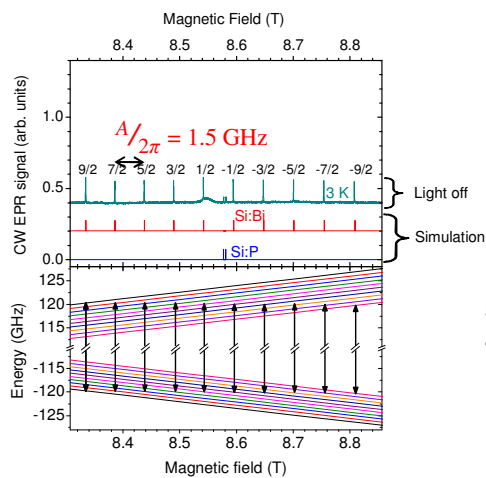


Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015



Bismuth donors in silicon

## ESR of Si:Bi at 240 GHz



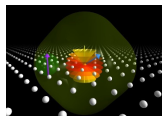
GWM, M Warner, AM Stoneham, PT Greenland, J van Tol, CWM Kay & G Aeppli, Nature Materials **9**, 725 (2010)

Si:P and Si:Bi resonances are resolved



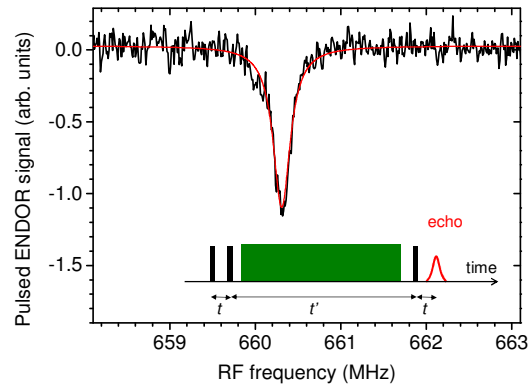
Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015





Bismuth donors in silicon

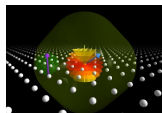
## Electron-nuclear double resonance (ENDOR) of Si:Bi at 240 GHz



GWM, M Warner, AM Stoneham, PT Greenland, J van Tol, CWM Kay & G Aeppli, Nature Materials **9**, 725 (2010)

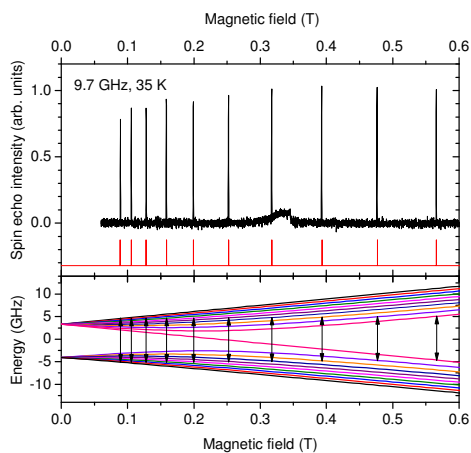


Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015



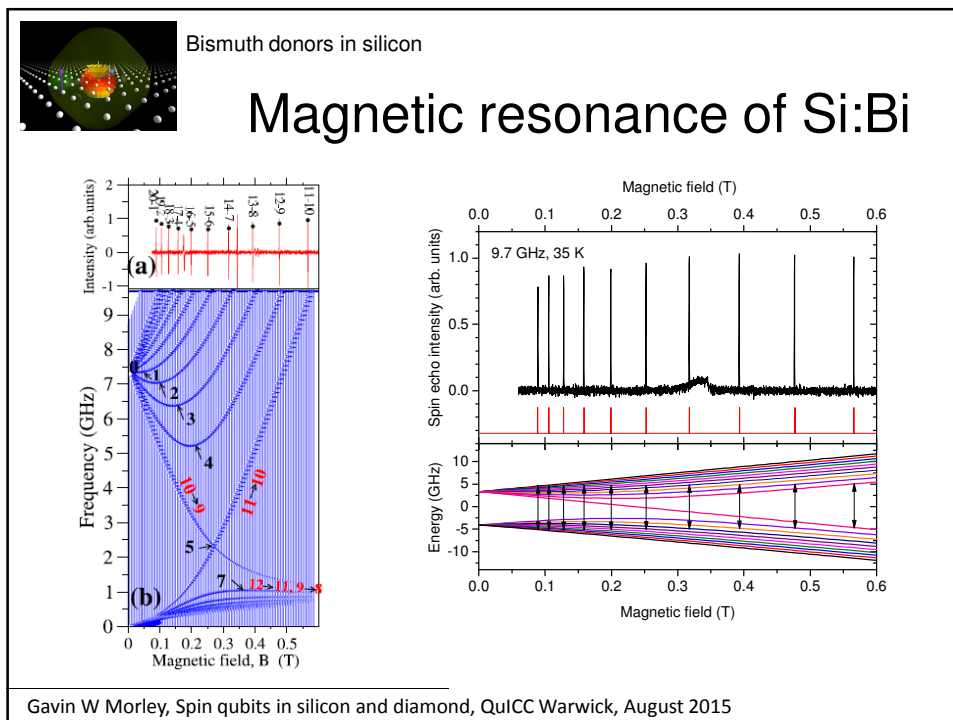
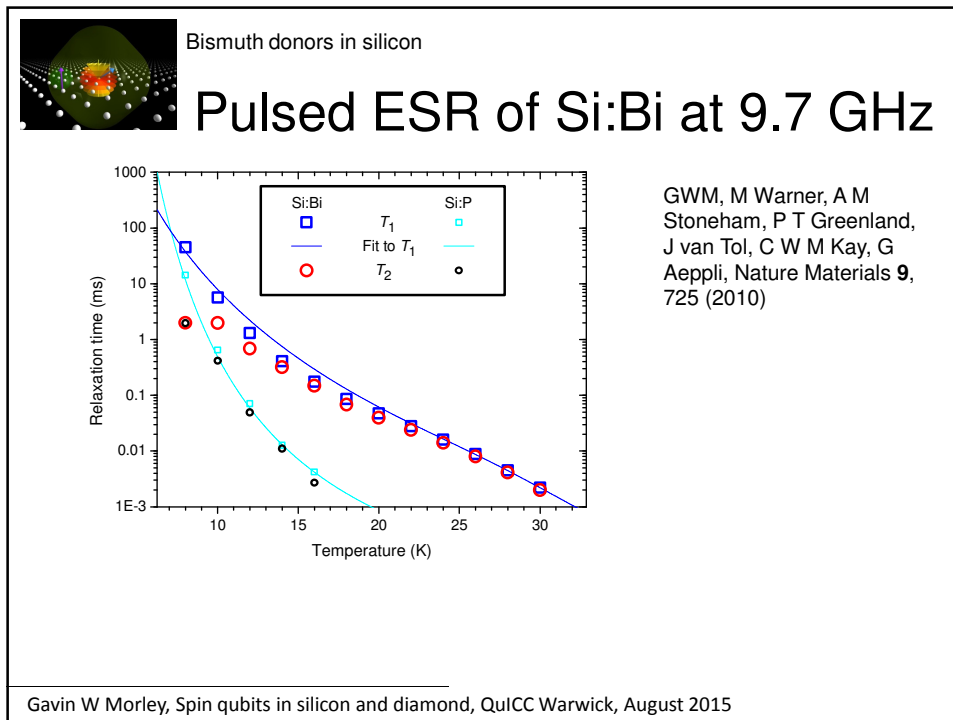
Bismuth donors in silicon

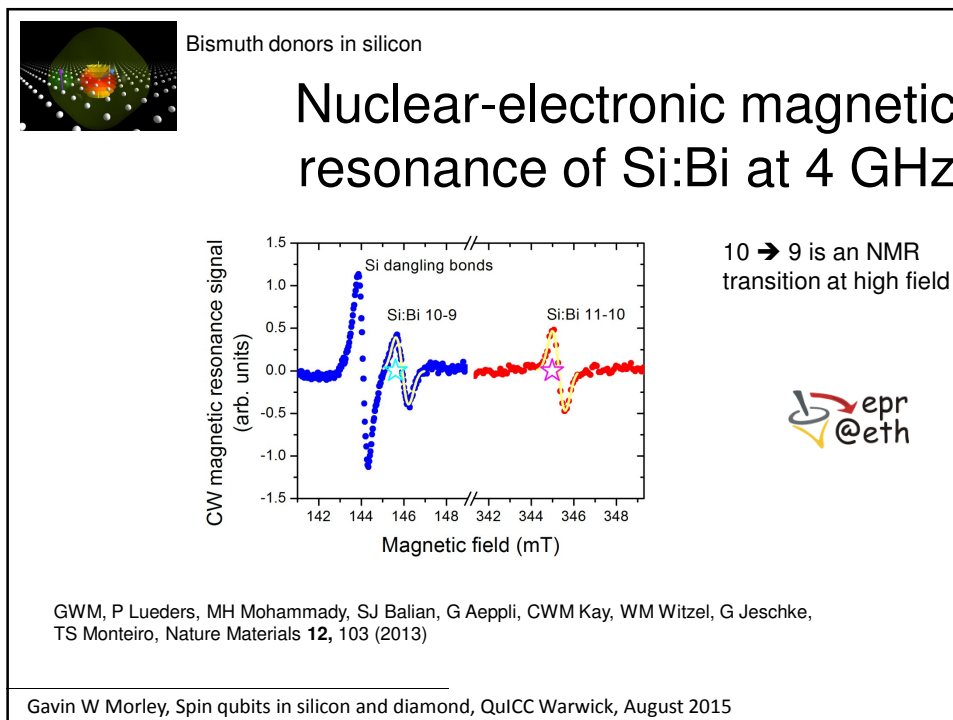
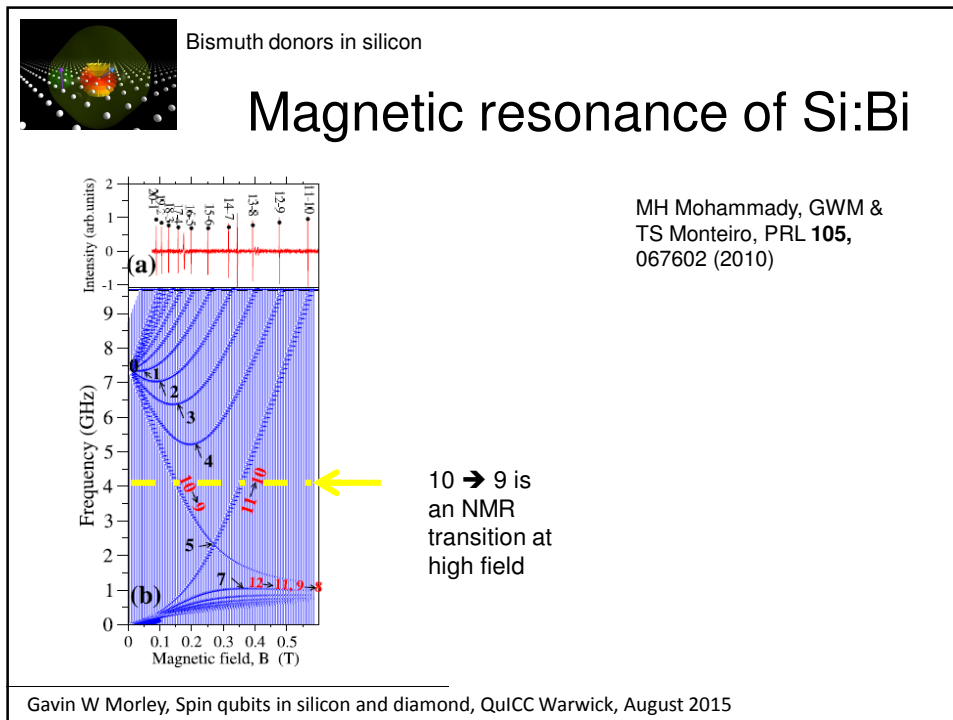
## ESR of Si:Bi at 9.7 GHz

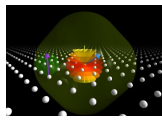


GWM, M Warner, AM Stoneham, PT Greenland, J van Tol, CWM Kay & G Aeppli, Nature Materials **9**, 725 (2010)

Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015

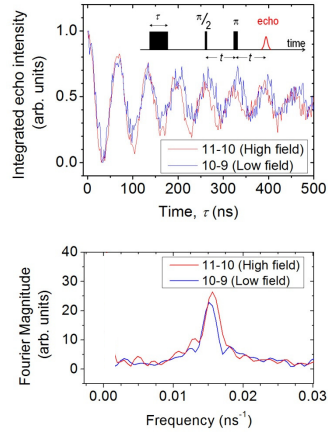






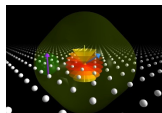
Bismuth donors in silicon

# Quantum control of a hybrid nuclear-electronic spin system



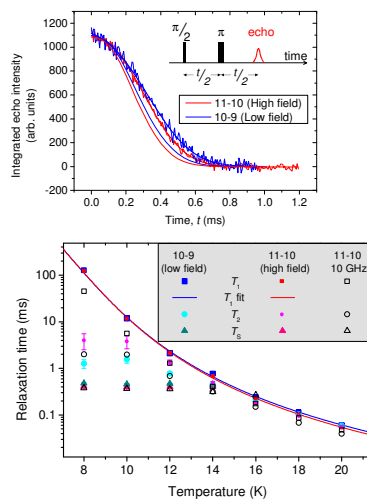
GWM, P Lueders, MH  
 Mohammady, SJ Balian, G Aeppli,  
 CWM Kay, WM Witzel, G Jeschke,  
 TS Monteiro, Nature Materials **12**,  
 103 (2013)

Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015



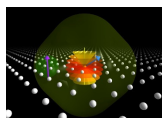
Bismuth donors in silicon

# Hybrid MR of Si:Bi at 4 GHz



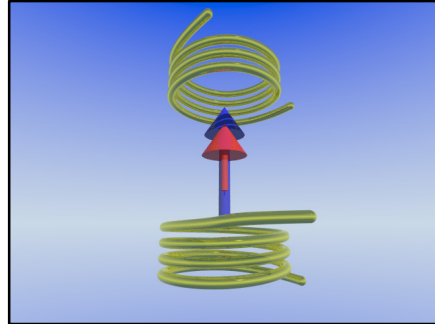
GWM, P Lueders, MH  
 Mohammady, SJ Balian, G Aeppli,  
 CWM Kay, WM Witzel, G Jeschke,  
 TS Monteiro, Nature Materials **12**,  
 103 (2013)

Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015



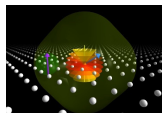
Bismuth donors in silicon

## Hybrid MR of Si:Bi at 4 GHz



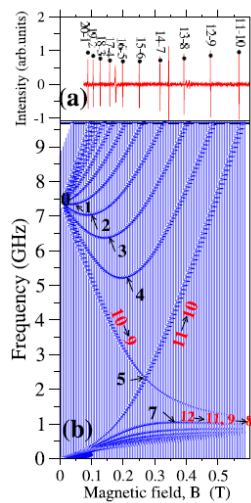
GWM, P Lueders, MH Mohammady, SJ Balian, G Aeppli, CWM Kay, WM Witzel, G Jeschke, TS Monteiro, *Nature Materials* **12**, 103 (2013)

Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015



Bismuth donors in silicon

## Si:Bi magnetic resonance



- T Sekiguchi *et al.*, PRL **104**, 137402 (2010)
- M Belli *et al.*, PRB **83**, 235204 (2011)
- S J Balian *et al.*, PRB **86**, 104428 (2012)
- M H Mohammady *et al.*, PRB **85**, 094404 (2012)
- C D Weis *et al.*, APL **100**, 172104 (2012)
- G Wolfowicz *et al.*, PRB **86**, 245301 (2012)
- P Studer *et al.*, ACS Nano **6**, 10456 (2012)
- P A Mortemousque *et al.*, APL **101**, 082409 (2012)
- G Wolfowicz *et al.*, Nature Nano **8**, 561 (2013)
- S J Balian *et al.*, PRB **89**, 045403 (2014)

Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015

## Donor qubits in silicon: conclusions

- Atomically-precise device fabrication
- Qubit initialisation
- Readout
- Control
- Coherence times
- Using Si:Bi offers extra benefits
- **Need to couple up two donors**

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Gavin W Morley, Spin qubits in silicon and diamond, QuICC Warwick, August 2015