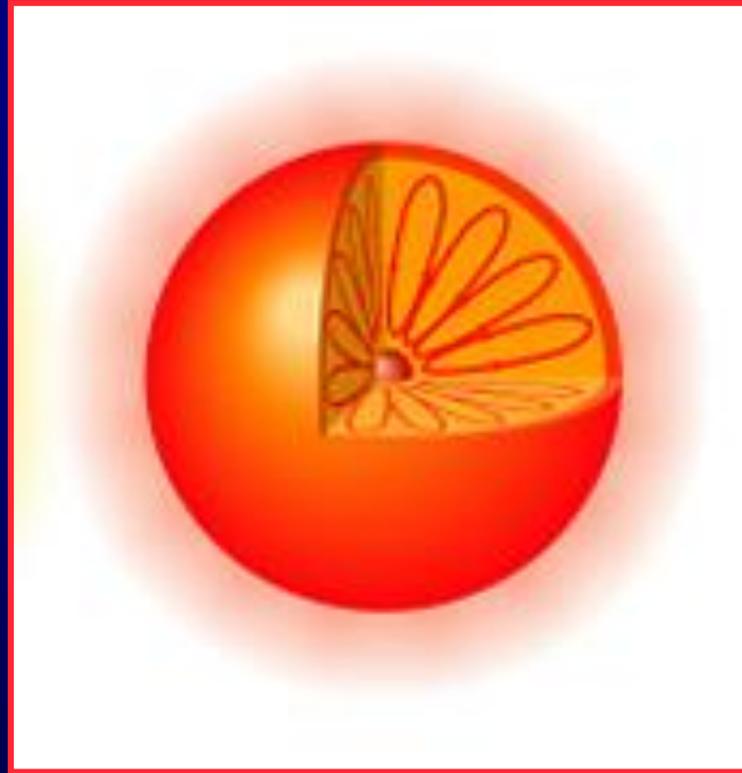


# Structure and evolution of M-dwarfs



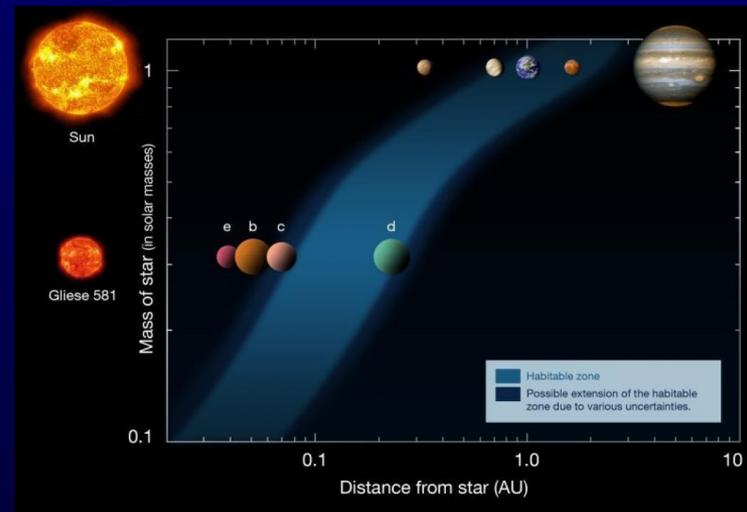
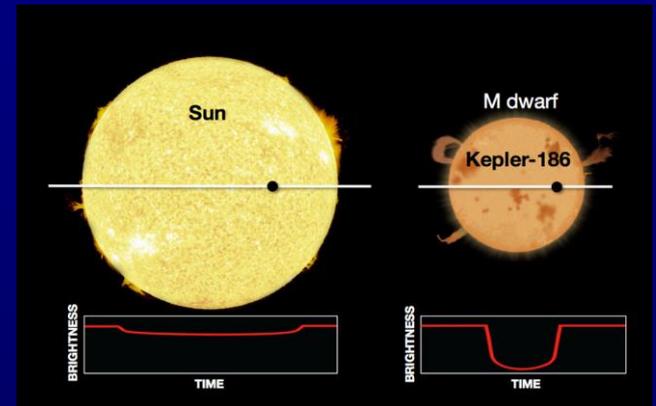
Maurizio Salaris

M-dwarfs comprise ~70% of all stars in the Galaxy and increase the chance of finding habitable planets through their sheer numbers and proximity to the Sun

Small planets are easier to detect via the radial velocity and transit techniques. Doppler shifts and photometric transit depths are larger due to the smaller star-to-planet mass and size ratios, respectively

Habitable zones are closer to the stars than those of Sun-like stars, increasing the probability to observe a transit

The extremely long lifetimes give ample time for biological development and evolution on orbiting planets

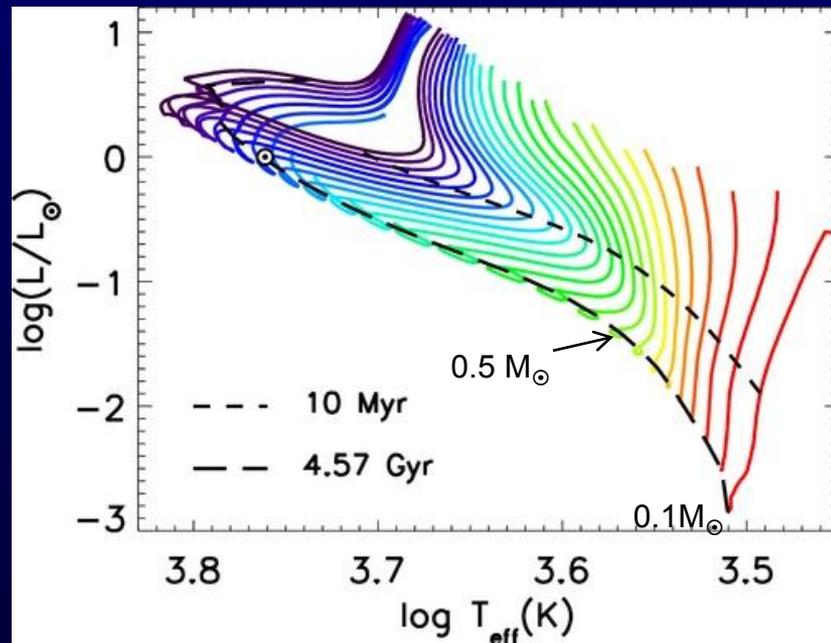


The theoretical counterpart of M-dwarfs are the so-called very-low-mass (VLM) stars, with masses between  $\sim 0.5 M_{\odot}$  (He-ignition limit) and  $\sim 0.1 M_{\odot}$  (H-burning limit). They are fully convective below  $\sim 0.35 M_{\odot}$

VLM are very dense, the Coulomb parameter  $\Gamma$  reaches values in the range 0.1-30 (as a reference,  $\Gamma > 180$  corresponds to the crystallization regime), meaning that Coulomb interactions among ions are very important.

Electron degeneracy becomes significant towards the H-ignition limit. Treatment of pressure ionization is crucial.

Molecular H, atomic He and several molecular species (e.g.  $H_2O$ ,  $CO$ ,  $VO$ ,  $TiO$ ) are stable in the atmosphere and outer envelope layers.



$0.1 \leq M/M_{\odot} \leq 1.25$  (in steps of  $0.05 M_{\odot}$ )

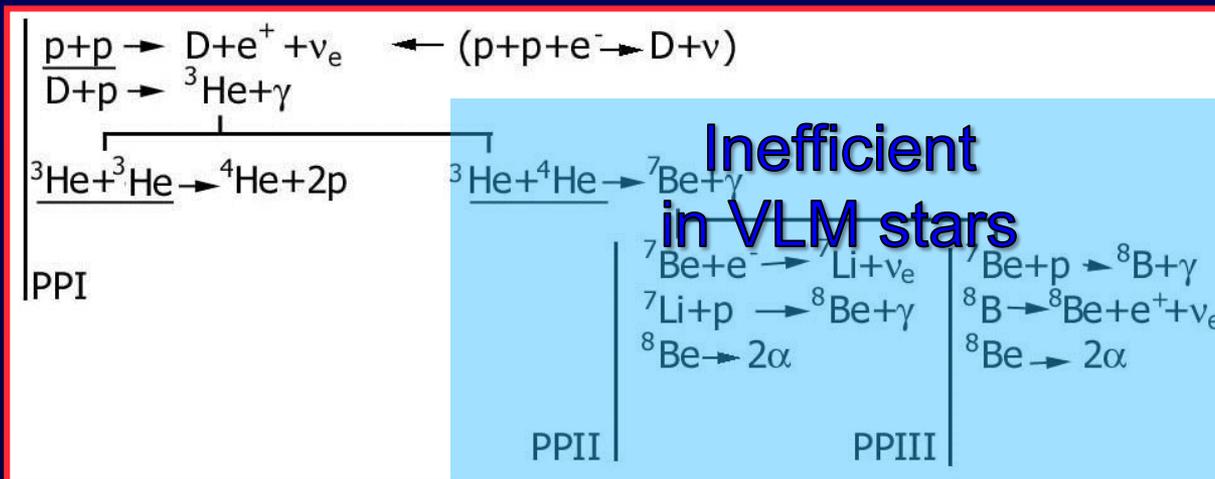
Spada et al. (2013)

- Extremely dense and cool objects

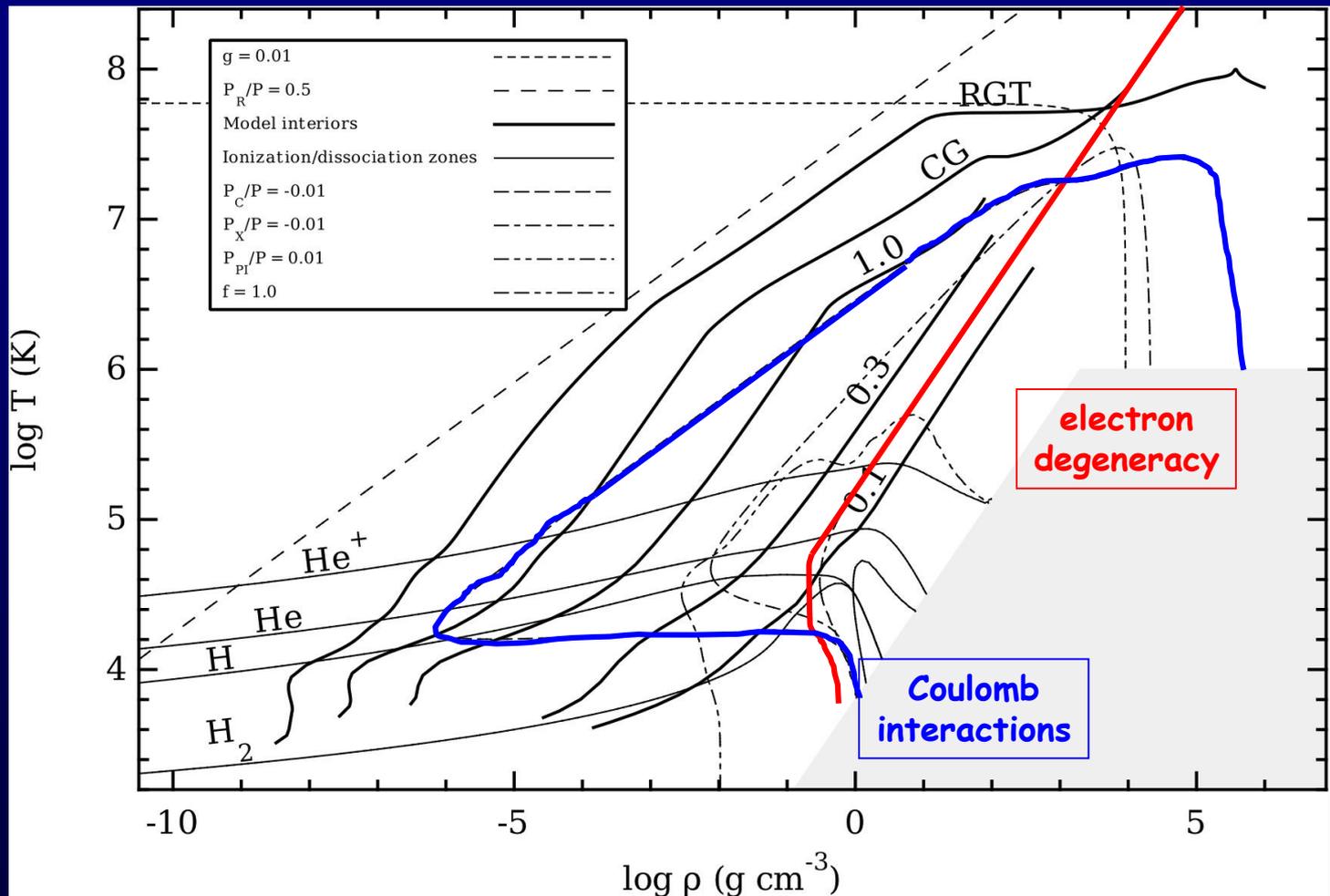
$M/M_{\odot}$	$T_c$	$\rho_c$	$T_{phot}$	$\rho_{phot}$
1.0	$\sim 1.6 \cdot 10^7 \text{K}$	$\sim 100 \text{g} \cdot \text{cm}^{-3}$	$\sim 6000 \text{K}$	$\sim 10^{-7} \text{g} \cdot \text{cm}^{-3}$
0.6	$\sim 10^7 \text{K}$	$\sim 150 \text{g} \cdot \text{cm}^{-3}$	$\sim 4000 \text{K}$	$\sim 10^{-6} \text{g} \cdot \text{cm}^{-3}$
0.1	$\sim 5 \cdot 10^6 \text{K}$	$\sim 500 \text{g} \cdot \text{cm}^{-3}$	$\sim 2800 \text{K}$	$\sim 10^{-4} \text{g} \cdot \text{cm}^{-3}$

EOS & opacity calculations in VLM regimes are complicated

- Models very sensitive to outer boundary conditions



# Equation of state



Outer boundary condition  $\longrightarrow$  Pressure (and T) at a reference optical depth  $\tau$

$$T^4 = \frac{3}{4} T_{eff}^4 (\tau + q(\tau))$$

$q(\tau) = 2/3 \longrightarrow$  Eddington grey

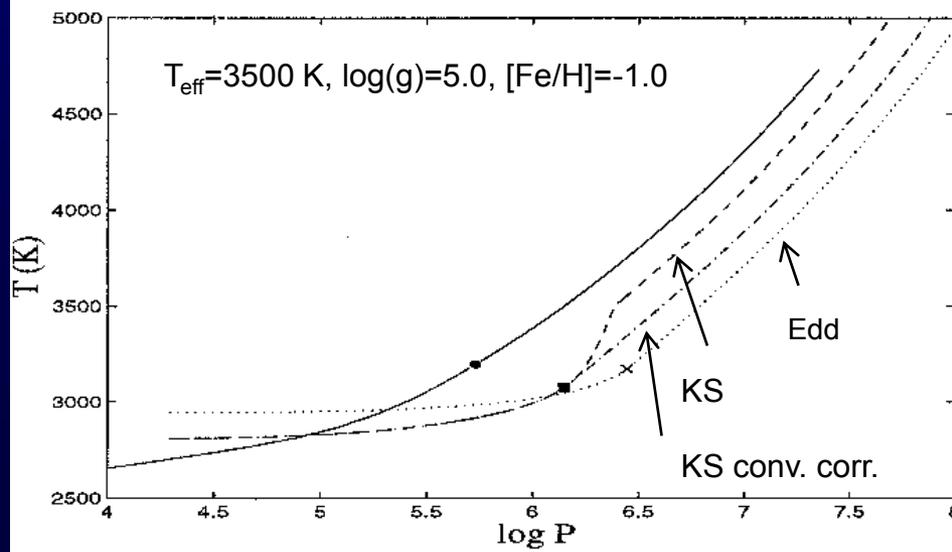
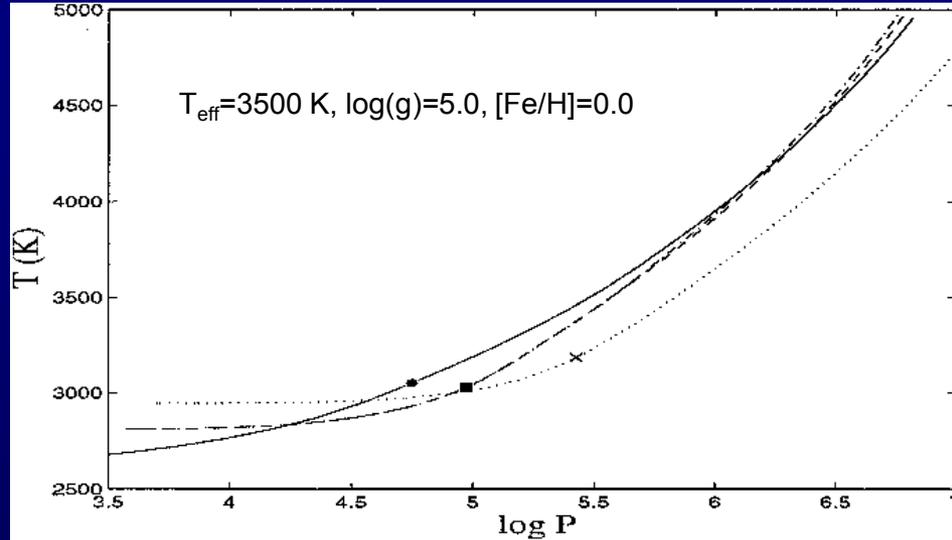
Krishna-Swamy (1966) gives a more complex  $q(\tau)$  based on the Sun to account for non-greyness

Heney et al. (1965) provide corrections for convection on  $T(\tau)$  relationships

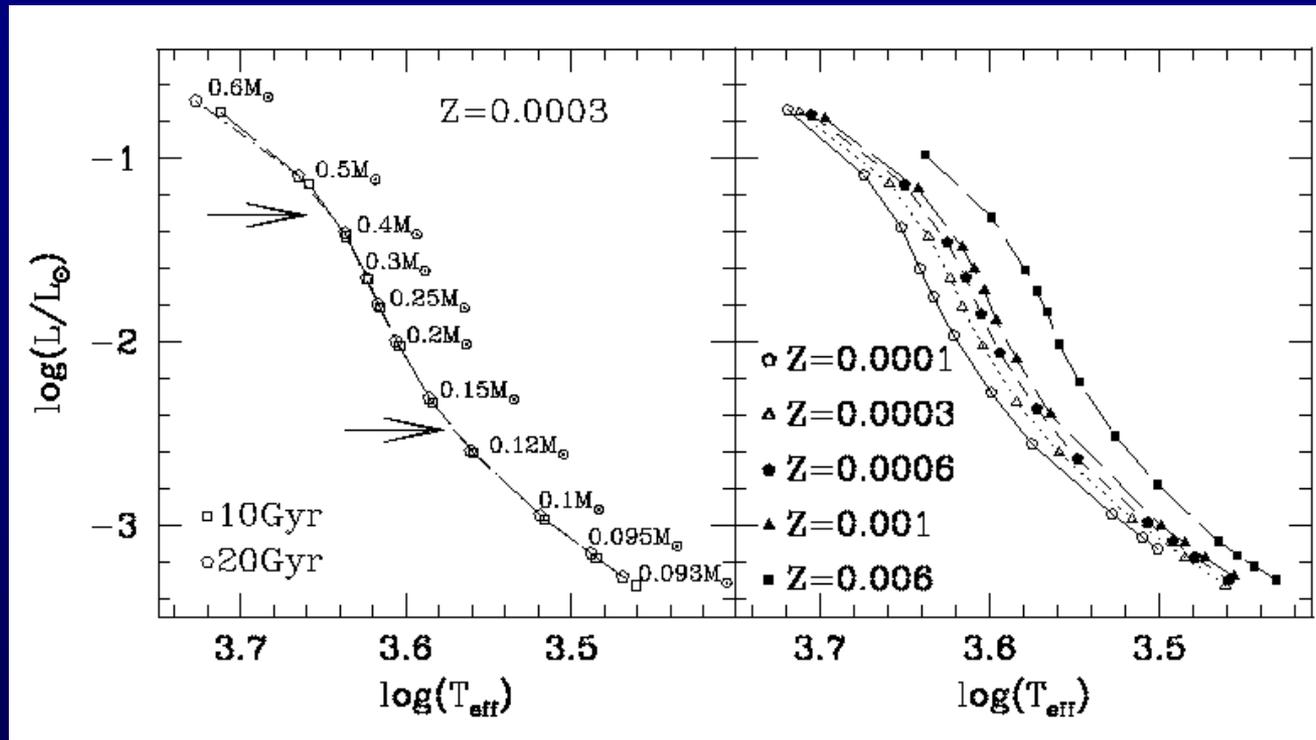
The values of  $(P_0, T)$  affect the interior thermal structure of VLM stellar models

The thermal stratification predicted by theoretical model atmospheres largely depends on the molecular and atomic opacities adopted in the computations

Chabrier & Baraffe (1997)



# The VLM stars' main sequence



The I bending point ( $T_{\text{eff}} \sim 4300\text{K}$  -  $M \sim 0.5M_{\odot}$ ) is due to the effect of  $\text{H}_2$  recombination

The II bending point ( $T_{\text{eff}} \sim 3000\text{K}$  -  $M \sim 0.15M_{\odot}$ ) is due to the increase of electron degeneracy. As a consequence, models approach their degenerate equilibrium radius ( $R \propto M^{-1/3}$ )

ation, in order both to investigate  
ting model atmospheres in stellar  
btain an indication of the value of  
 $T_{\text{eff}}^{\text{crit}}$ . Figs 2 and 3 show the results of  
expected, even a quick inspection of  
t at effective temperatures around  
is achieved between the different  
e extension of B95 with Kurucz  
when  $Z=0.002$  one may notice in  
transition, between the  $T(\tau)$  stellar  
es, which occurs at  $T_{\text{eff}} \approx 4400$  K for  
he same smooth transition occurs  
B95 models at  $T_{\text{eff}} \approx 4000$  K for a  
finding appears to be in good agree-  
Brett (1995a, his fig. 8) when com-  
spheres with the ATLAS9 results.  
 $T_{\text{eff}} < 4000$  K the K93 model sequence  
 $T(\tau)$  models is simply a result of the  
n the Kurucz (1993) model atmo-  
models computed by adopting the  
on are hotter and brighter than the  
rger discrepancy is present at

B95 models agree with K93 ones at  $T_{\text{eff}}$ .  
mum discrepancy between the  $T(\tau)$   
structures computed by adopting acc  
spheres appears at  $T_{\text{eff}} \approx (4100-4200)$ .  
differences of the order of  $\approx 180$  K in  $T$   
 $L_{\odot}$ .

### 3 STELLAR MODELS

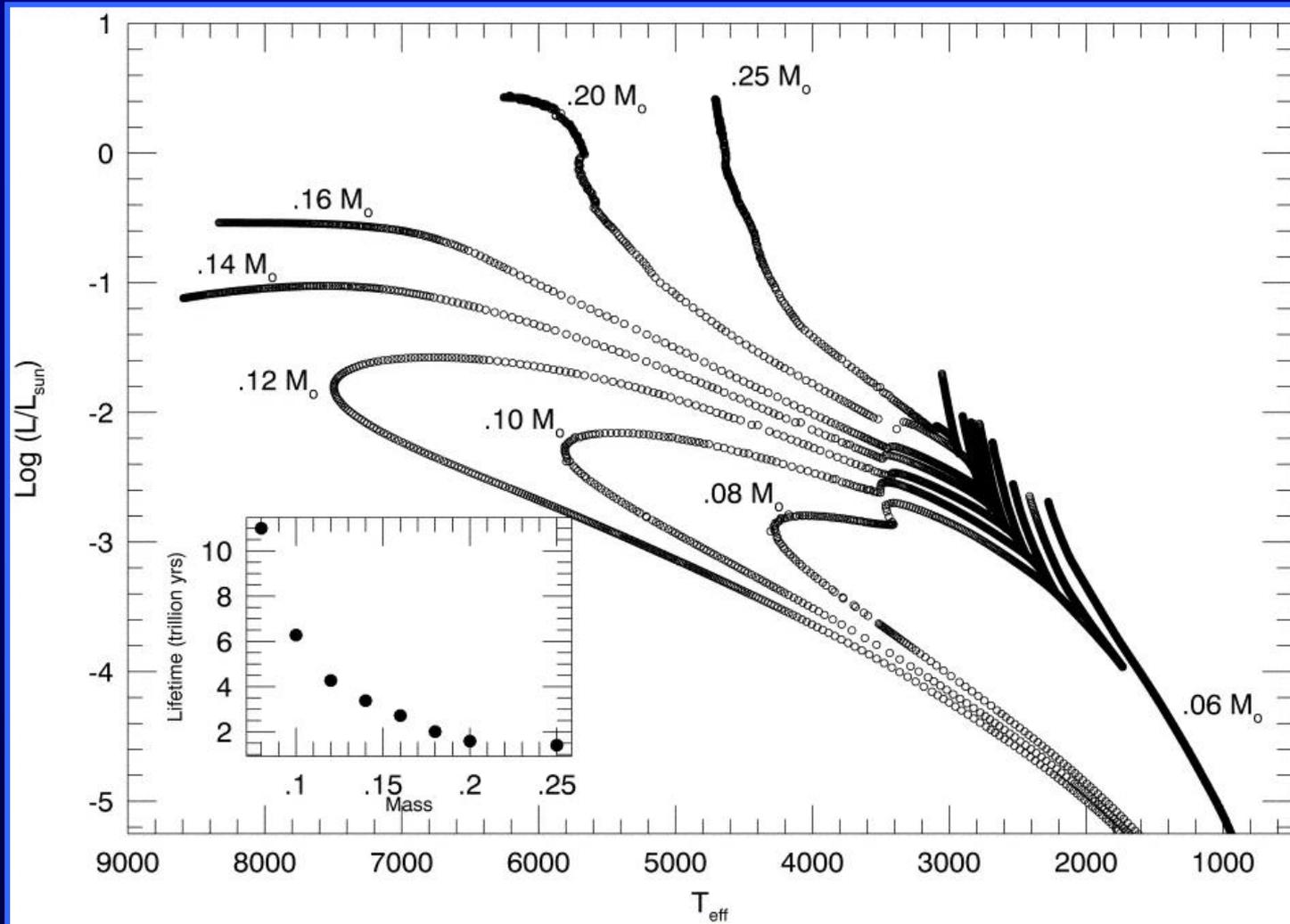
For each given metallicity, we sele  
sequence of models the one obtained  
proper range of validity) the  $T(\tau)$ , K  
models, ensuring that a fine and smoot  
between the models computed under di  
about the outer boundary conditions. Fi  
of present 'best' MS in the HR diagr  
assumptions about metallicity. Tables 1  
sity, effective temperature, absolute vis  
predicted colours (in the standard Johns  
 $VRI$  and the CIT system for  $K$ ) fo  
models for the various selected metal  
and colours have been evaluated by a

# Effect of boundary conditions on the H-R diagram

## *Stellar models for VLM stars* 713

and only minor changes for stars with mass around  $0.6 M_{\odot}$ .  
Since in the present work we are mainly dealing with stellar  
models with mass  $M \leq 0.6 M_{\odot}$ , the results are not affected  
by the choice of the mixing length parameter. Moreover, as  
far as concerns the model atmosphere computations, B95  
has clearly shown that a variation of the mixing length  
parameter in the range 1.0 to 2.0 produces only minor  
effects at effective temperatures around 4000 K, and that  
these structural effects decrease rapidly, therefore decreas-  
ing the effective temperature of the model.

# The long-term evolution of VLM stars



Laughlin et al. (1997)

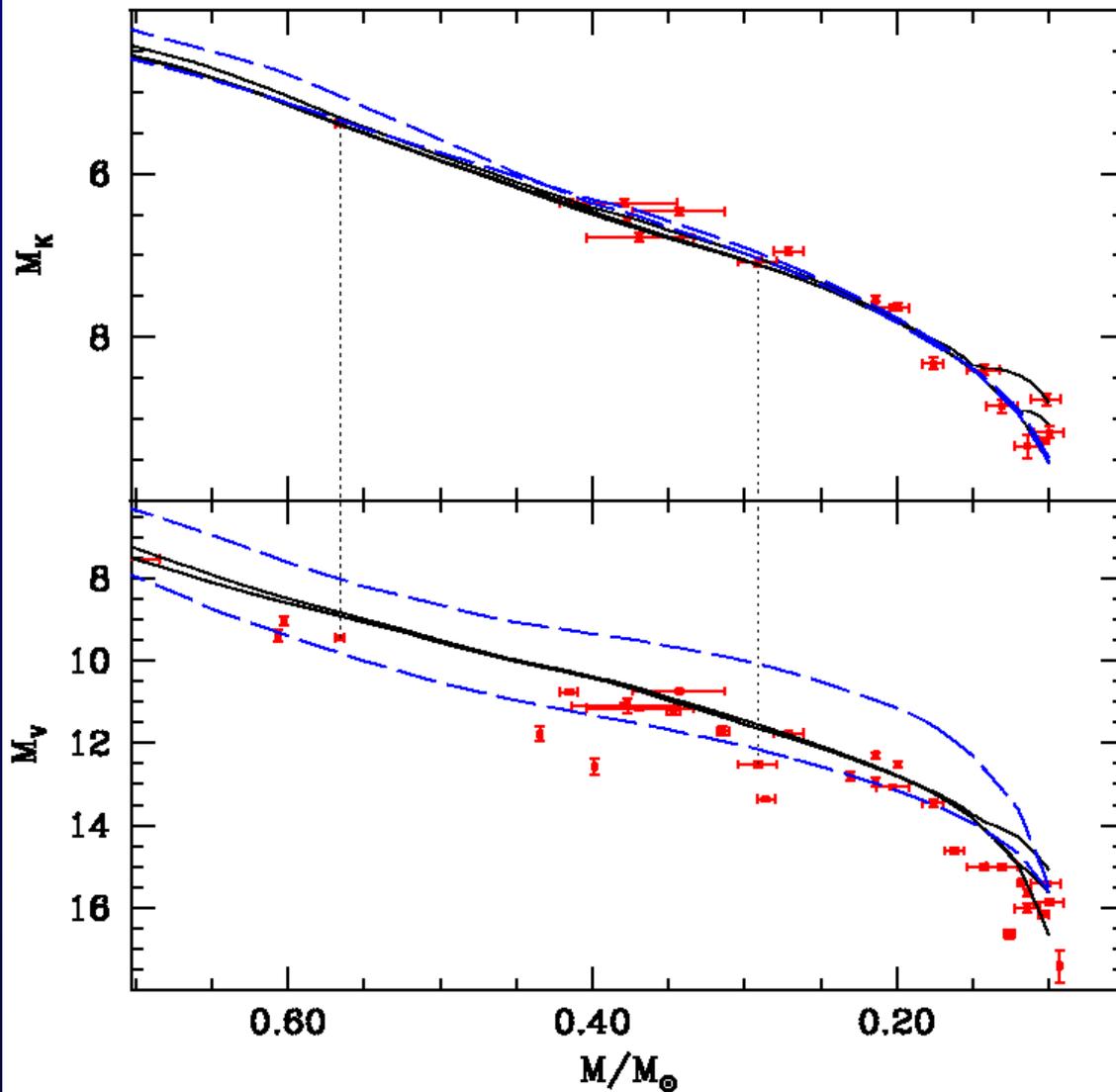
We have just completed the calculation of a first baseline, state-of-the-art set of standard (no-rotation, no magnetic fields) VLM models, from the pre-MS until ages  $\sim 15$  Gyr, for a large range of initial metallicities (scaled-solar metal mixture). This is part of the wider scope new BaSTI project

People directly involved (WP121 110):

- Santi Cassisi (INAF - Collurania Astronomical Observatory - Italy)
- Maurizio Salaris (ARI, Liverpool John Moores University - UK)
- Adriano Pietrinferni (INAF - Collurania Astronomical Observatory - Italy)

Are current VLM stellar models reliable?

# Mass-luminosity relationships

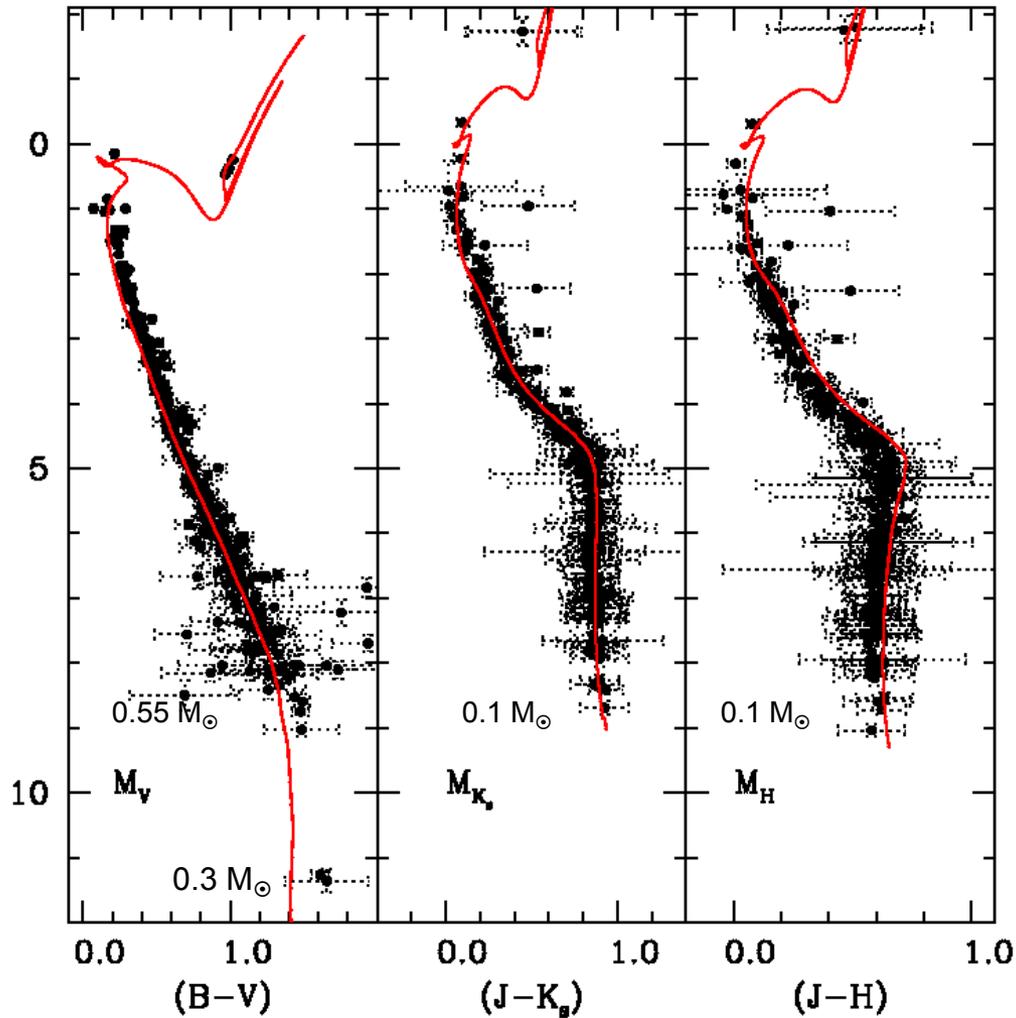


[Fe/H]=0.06  
300 Myr, 1Gyr, 10  
Gyr (black)

[Fe/H]=-0.4, +0.4  
10 Gyr (blue  
dashed)

Data from Delfosse  
et al. (2000)

# VLM stars in the Hyades

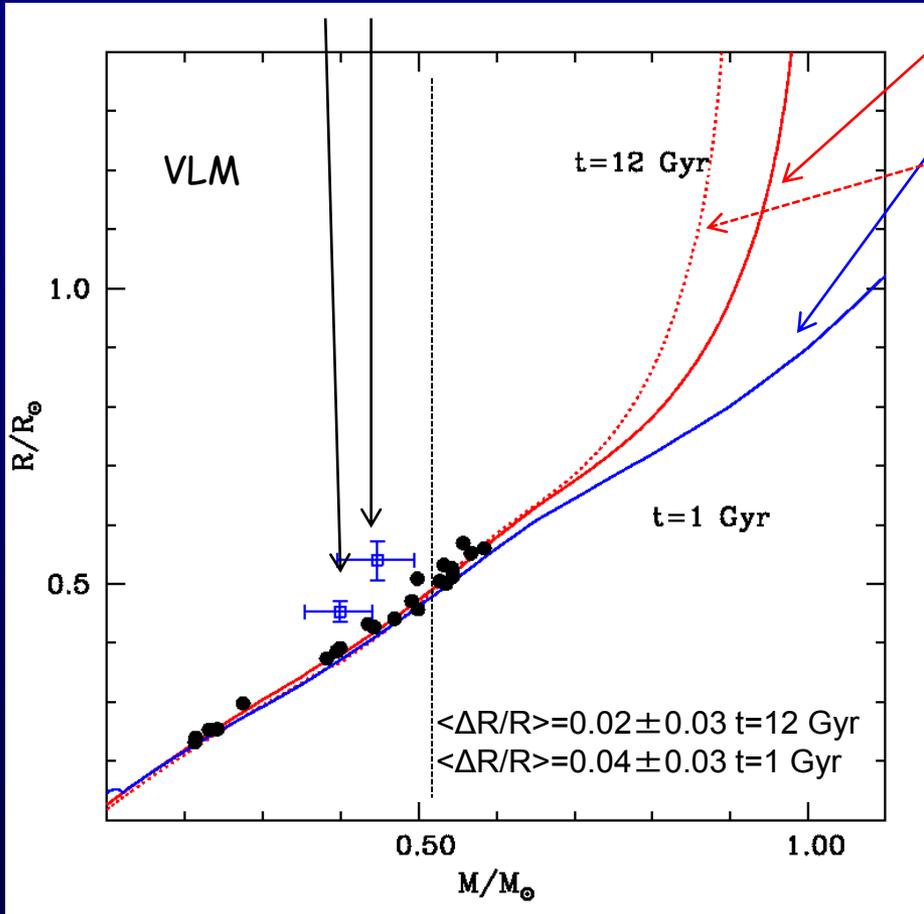


2MASS data from  
Kopytova et al. (2016)  
Optical data from Röser et  
al. (2011)

900 Myr, [Fe/H]=0.06

## Unevolved components

KELT J041621-620046



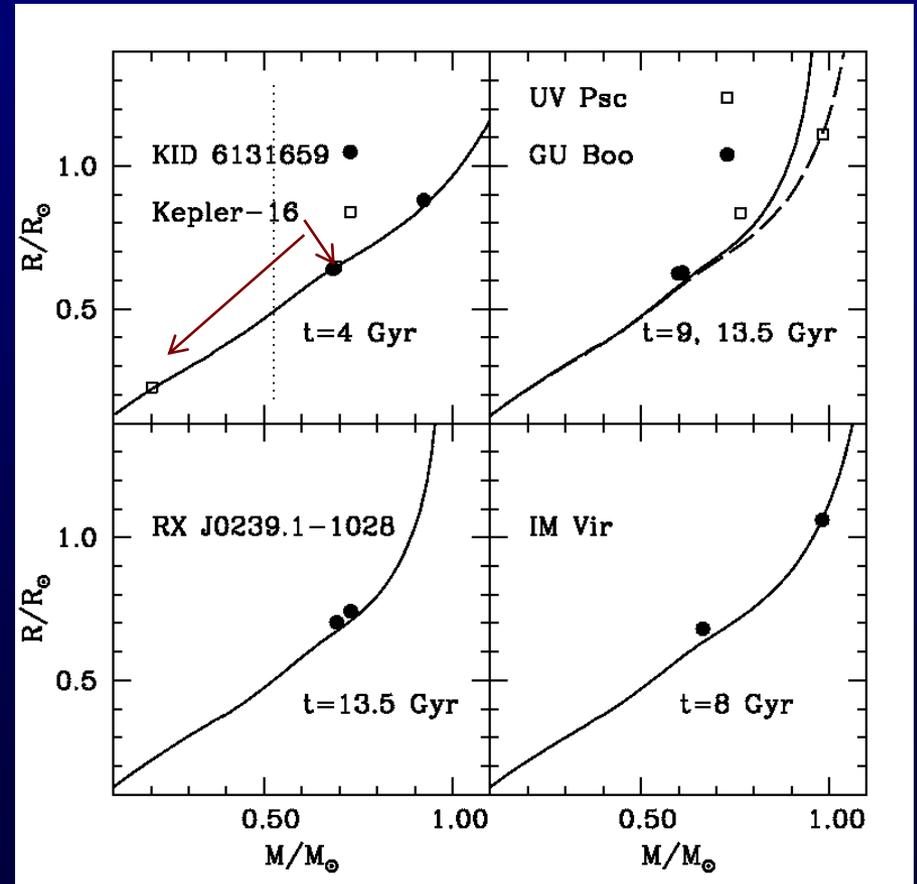
## Mass-radius relationship

$[Fe/H]=0.06$

$[Fe/H]=-0.40$

At least one evolved component

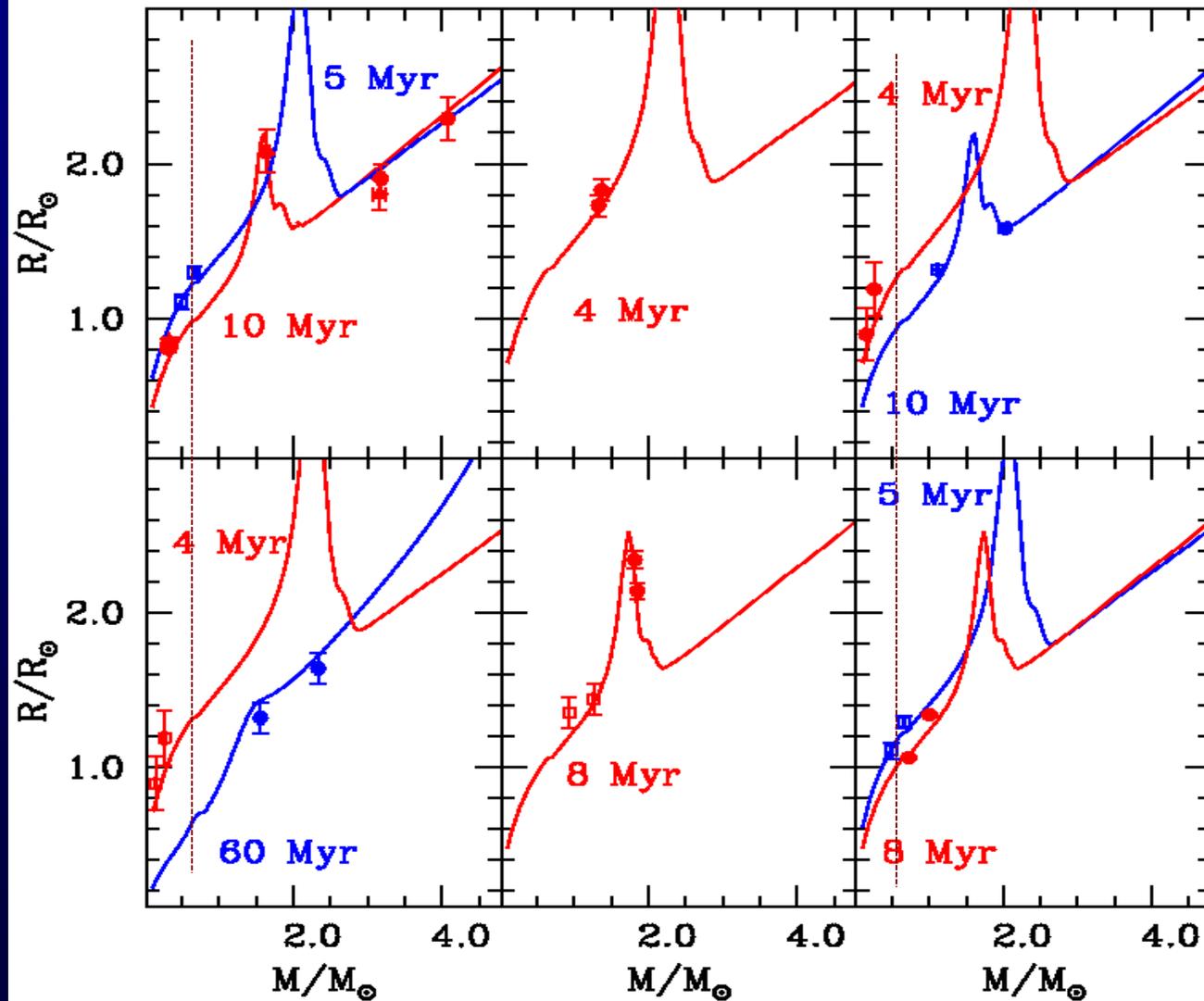
$[Fe/H]=0.06$



DEB data compiled by Feiden & Chaboyer (2012 - random mass and radius uncertainties less than 3%) + Lubin et al. (2017)  
 Systematic uncertainties on determinations of  $R$  are likely  $\sim 3\%$  (discussion in Feiden & Chaboyer 2012)

# Pre-MS VLM

[Fe/H]=0.06



Data from Stassun et al. (2014)

## Conclusions and WP121 110 roadmap

For several observed VLM stars there isn't a clear discrepancy with radii predicted by our baseline models. In other cases systematics do appear clearly. They are likely correlated with the strength of magnetic activity (Spada et al 2013)

Extend comparisons of our baseline models to additional datasets

Calculate baseline  $\alpha$ -enhanced model grid

Calculate rotating VLM models (rotation already included in the code)

Include magnetic field effects, following Feiden & Chaboyer (2012) methods