

A Spectral Approach to TTVs

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ApJ submitted

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“Classical” approach

- Fit planetary parameters and all $T_{\text{mid},i=1..N}$ simultaneously.
 - Recent major work: Kepler TTVs catalog by Holczer+2016

- Limitations of classical approach

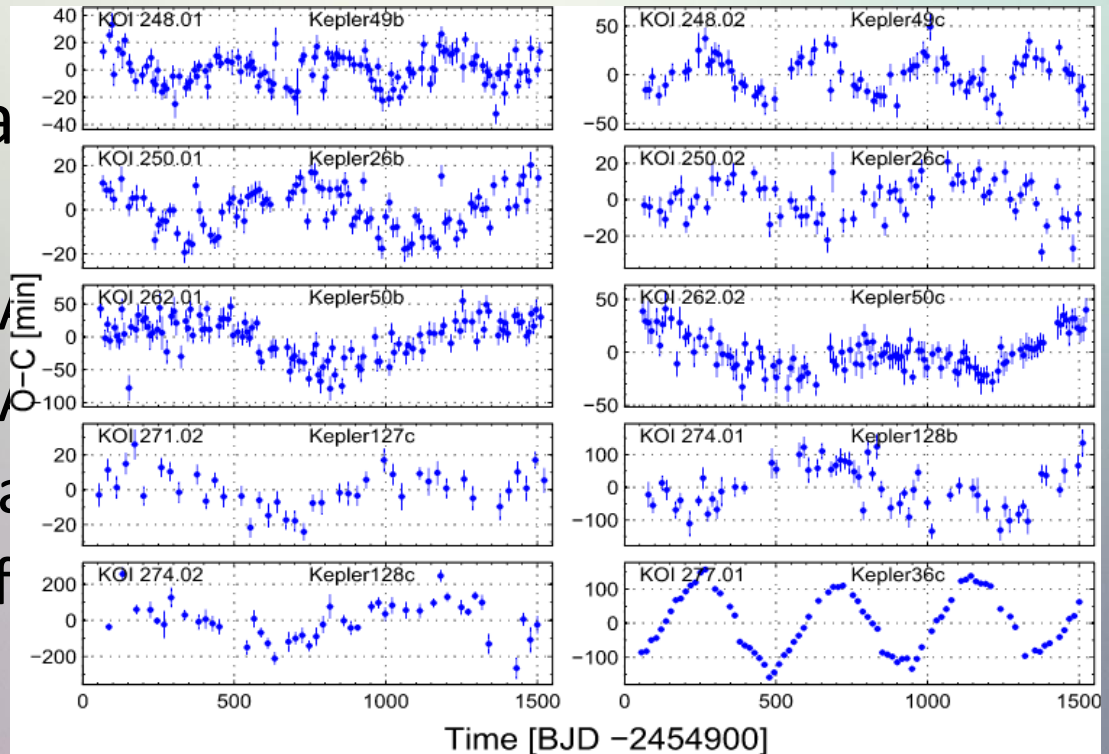
- Strong Biases:

Deep transits (ΔA)

Long periods (P)

- Blind to short-transits

- Large number of false positives



Spectral approach to TTVs

Lessons learned:

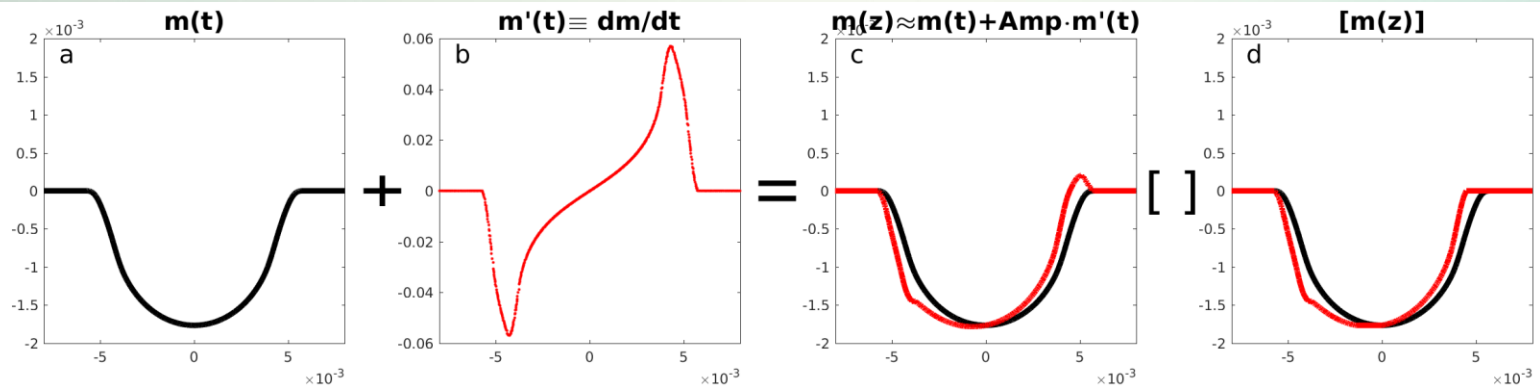
- Linear ephemeris means: $T_{\text{mid},i} = T_0 + iP$
- TTV information approx. sinusoidal

A new way to look for TTVs:

- $T_{\text{mid},i} = T_0 + iP + A_{\text{TTV}} \cdot \sin[2\pi t f_{\text{TTV}} - \varphi_{\text{TTV}}]$
- Check: did it improve χ^2 relative to χ^2_{linear} ?
- Scan over $A_{\text{TTV}}, f_{\text{TTV}}, \varphi_{\text{TTV}}$
- WORKS! But.... Problematic search space.

Perturbative Approximation (PA)

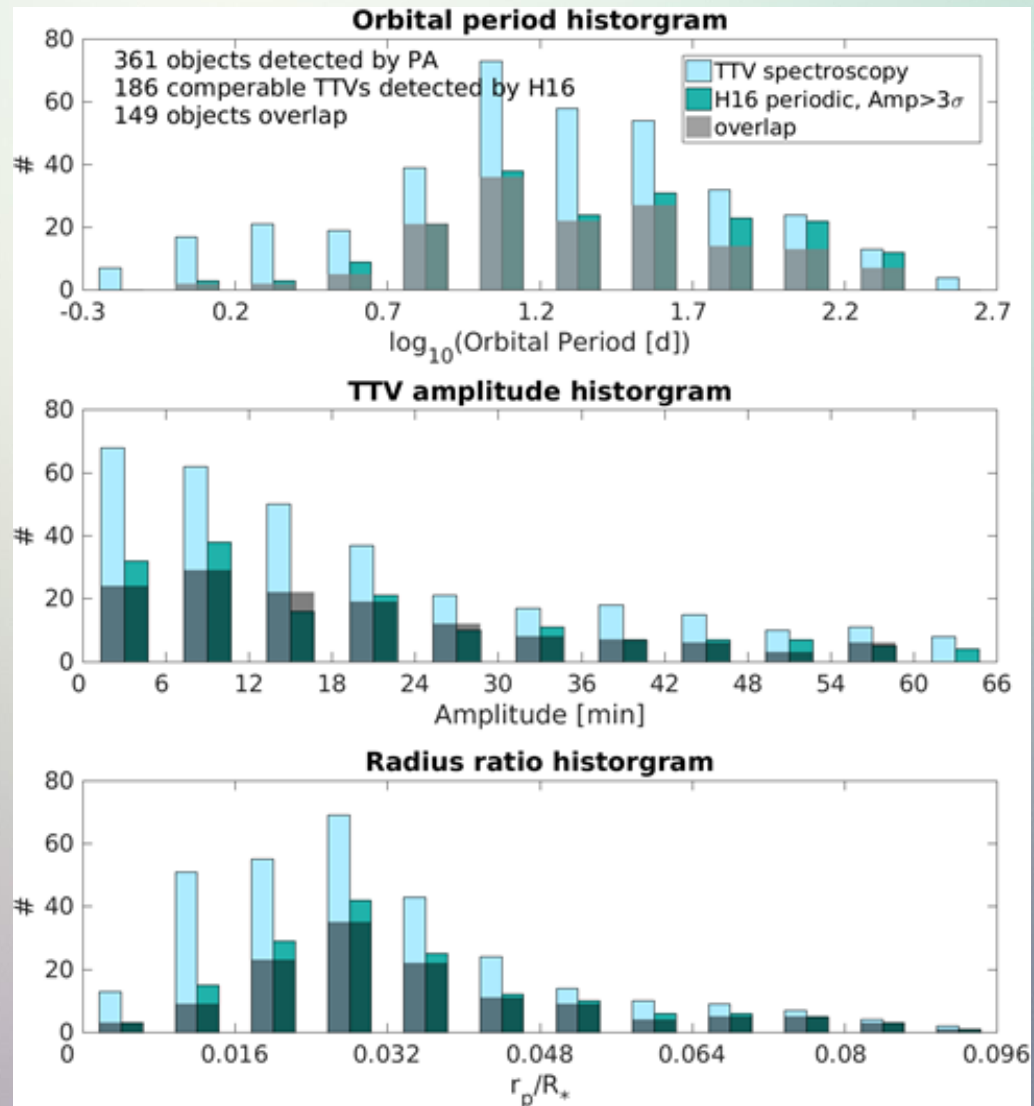
- Large-amplitude TTVs probably already found



- Add two perturbation: $f=\text{sine}$ & $g=\text{cosine}$:
$$m_i(z_i) \approx m_i(x_i) + A f_i m'_i + B g_i m'_i$$
- Would fit both φ_{TTV} and A_{TTV} analytically
- Sensitive, nearly unbiased, fast

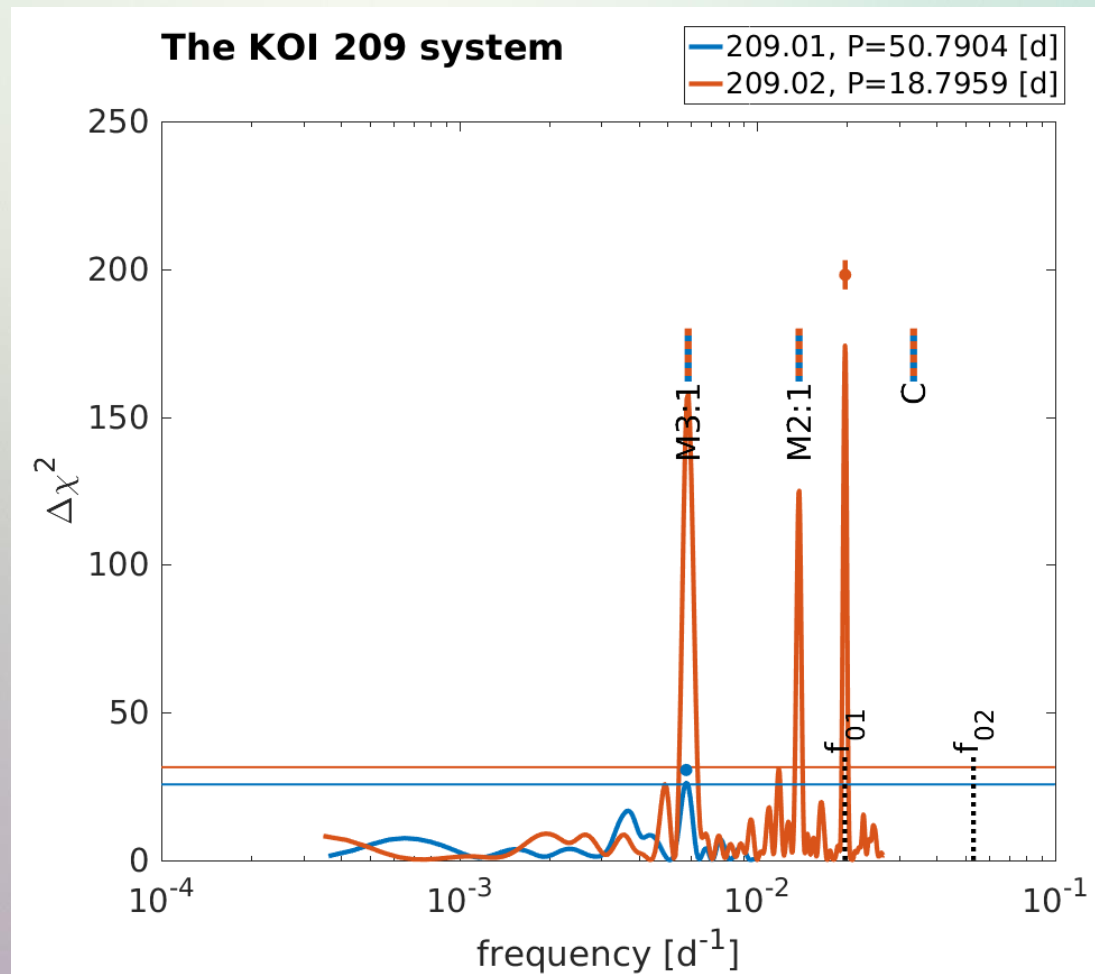
Kepler Results - statistics

- Required Bootstrap confidence ≥ 0.999
- 131 new TTVs in (+2/3 over H16*)
- Depth:
 - All KOIs: 428ppm
 - PA: 458ppm
- Period:
 - All KOIs: 9.5d
 - PA: 10.8d



Results - Examples

- KOI-209 (Kepler-117): text-book example

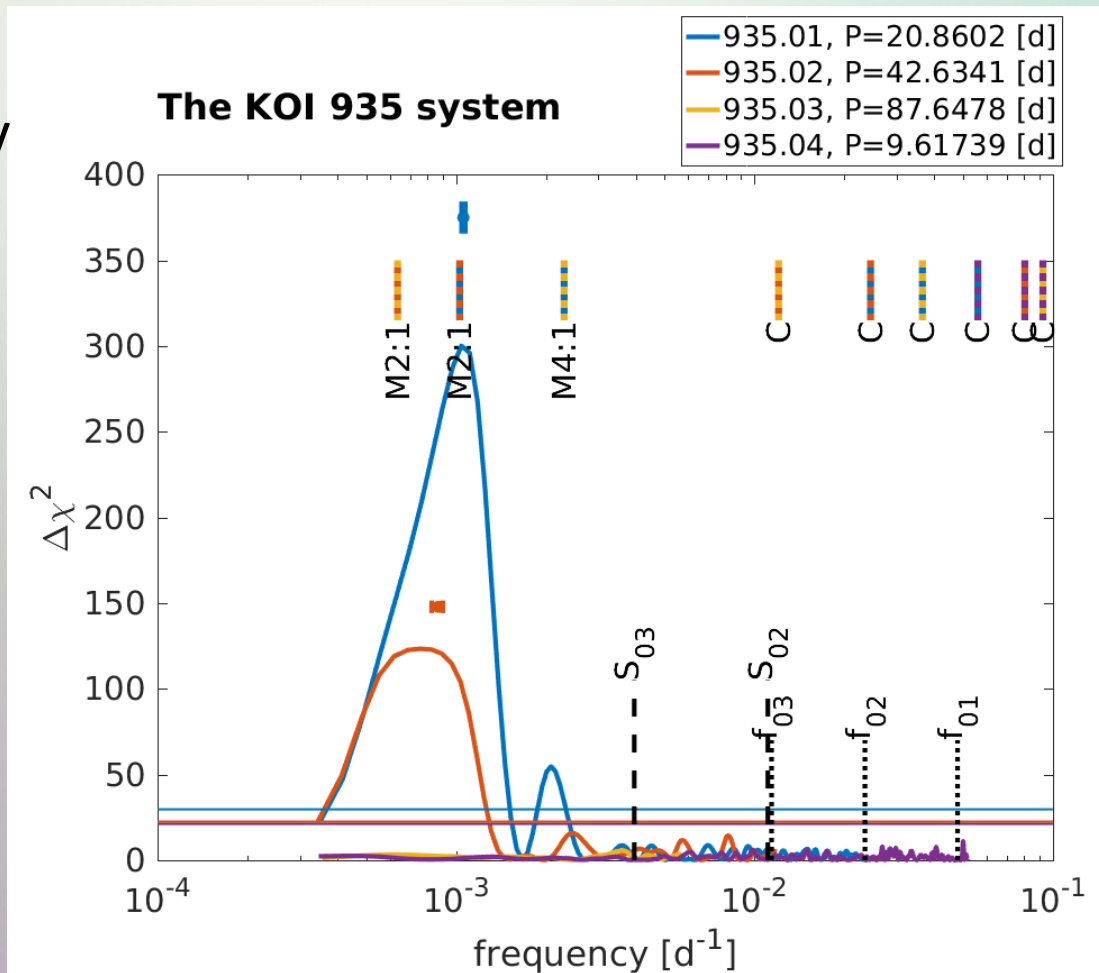


Results - Examples

- KOI-935 (Kepler-31)

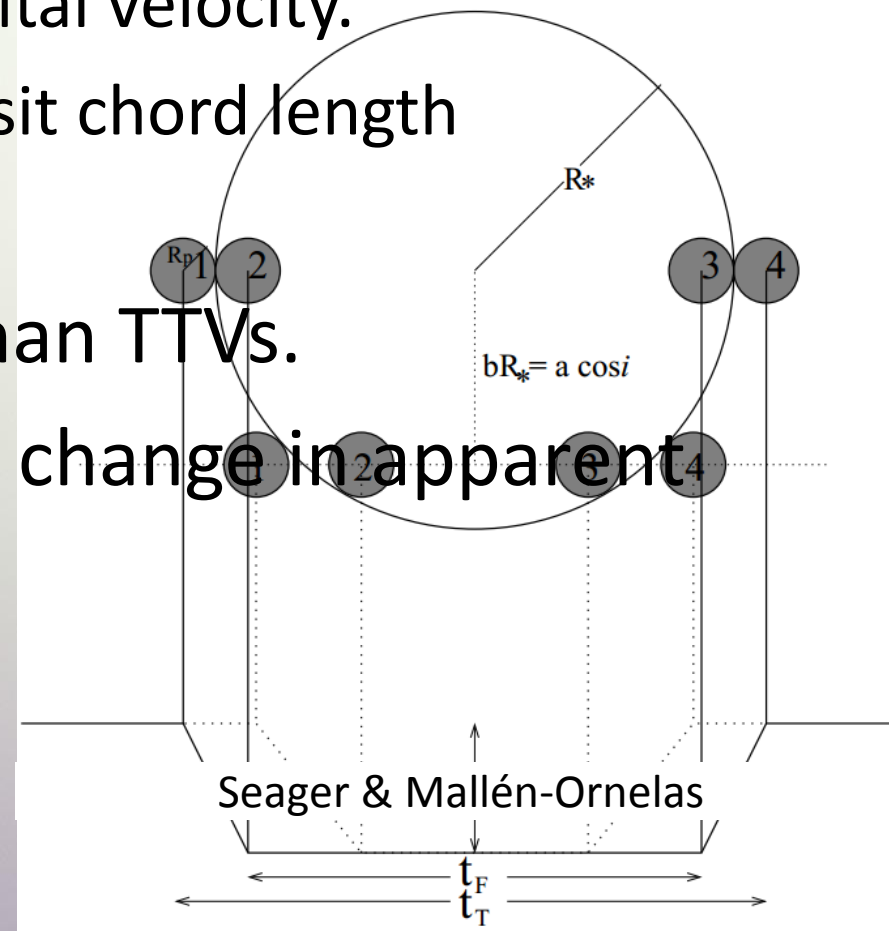
- .01-.02: main .01 peak
- .01-.03: new secondary
- .02-.03: wide .02 peak

1:2:4 resonant chain
w/masses?



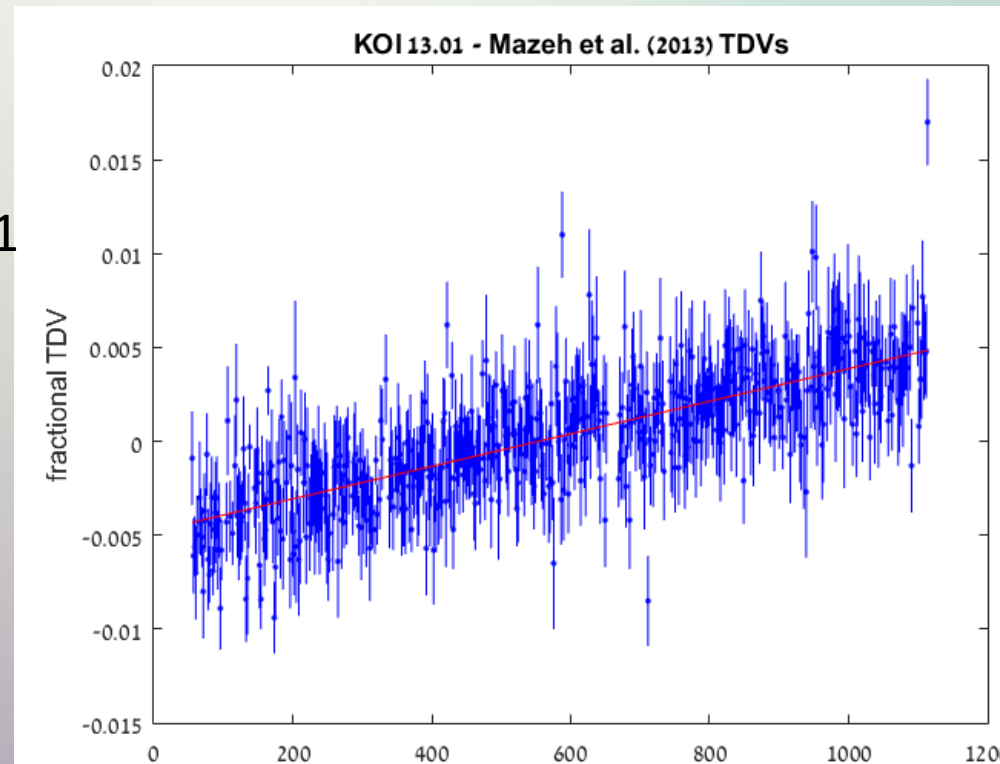
TDVs: Transit Duration Variations

- Origin of TDVs is:
 - Change in tangential orbital velocity.
 - Change in apparent transit chord length
 - Both simultaneously
- Noisier measurement than TTVs.
- TbVs are only caused by change in apparent transit chord length.
- PA: linearly perturb b



KOI 13.01 TDV/TbV

- Mazeh+13 catalog (Q1-Q12 data):
fractional TDV of $0.00316 \pm 0.00012 \text{ yr}^{-1}$.
- Circular orbit $\rightarrow \text{TbV} = \frac{(1-b^2)}{-b} (\text{Frac. TDV}) =$
 $= -0.00142 \pm 6e-5 \text{ yr}^{-1}$
- PA gives TbV
 $= -0.00130 \pm 5.9e-5 \text{ yr}^{-1}$
(Preliminary analysis)



Conclusions

- Spectral Approach is a new TTV detection technique, allowed many new detections.
- Its PA generalizable to other transit variations.
- Unbiased, sensitive, general, very fast.
- May contribute to M-R relation of small planets
- First-line detector of TTVs/TbVs/...: very suitable to short-baseline datasets like: TESS, PLATO, ...

Thank you.